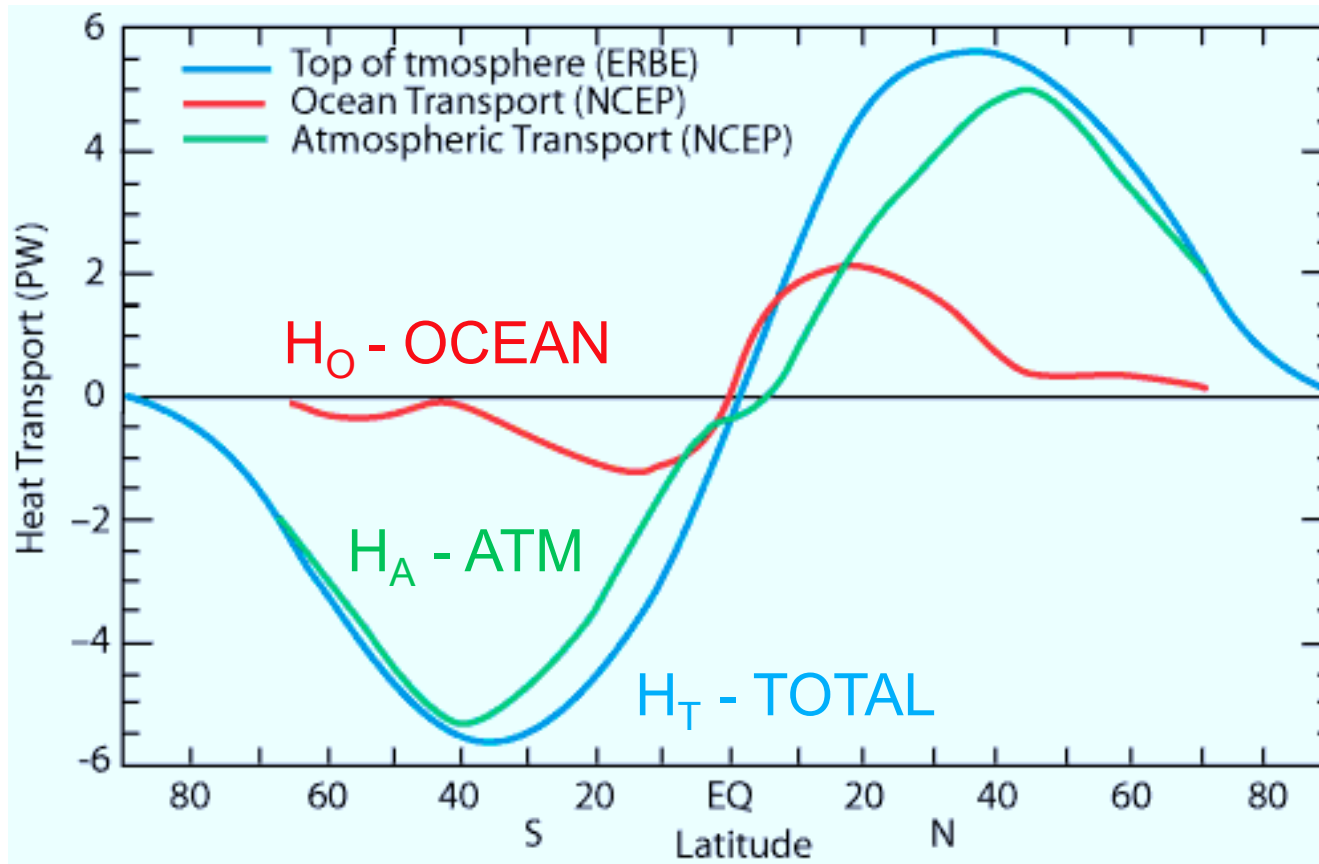


# Earth's Energy Budget, Heat Transport, and Ice

## Northward (or Meridional) Heat Transport

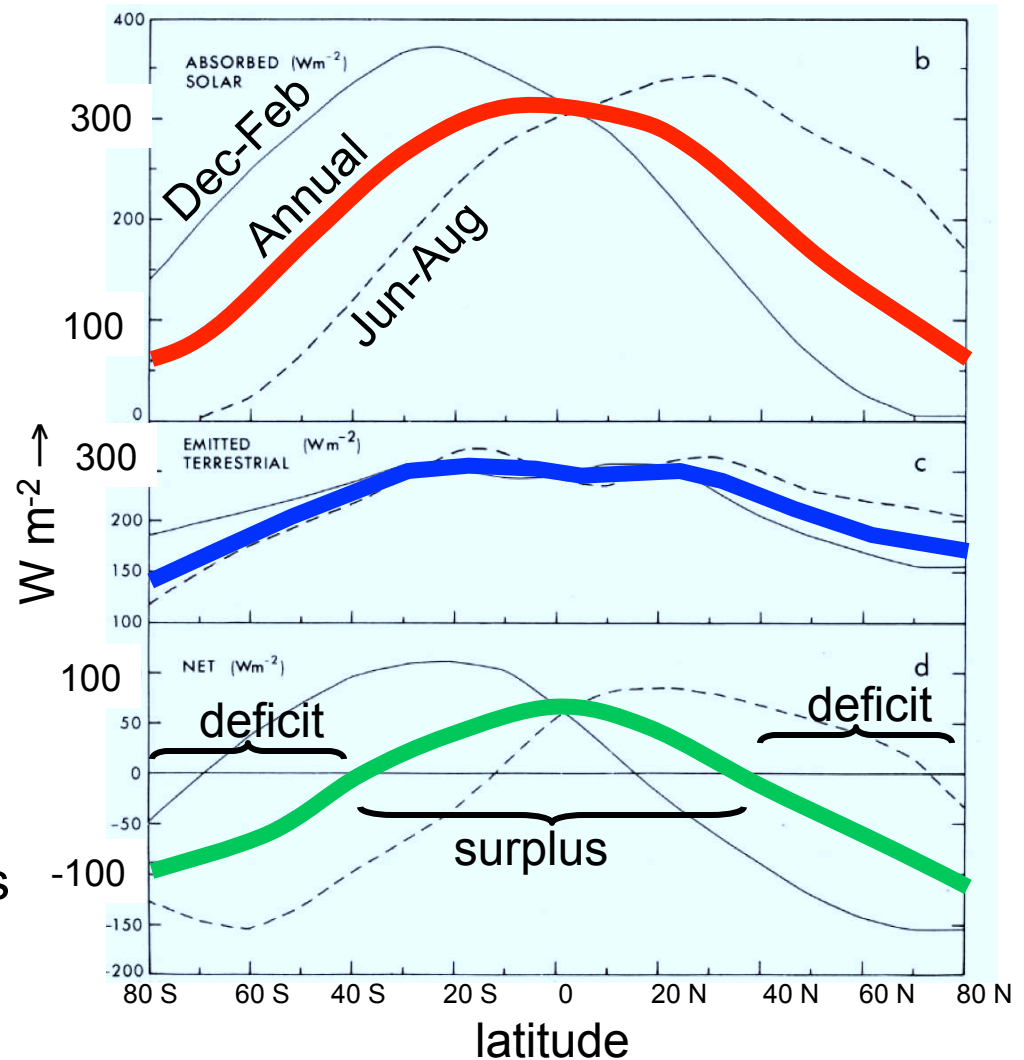


# Annual mean Top Of Atmosphere (TOA) radiation budget of planet

Absorbed solar,  
 $Q_0(1-\alpha)$ :  
 $\alpha$  = albedo

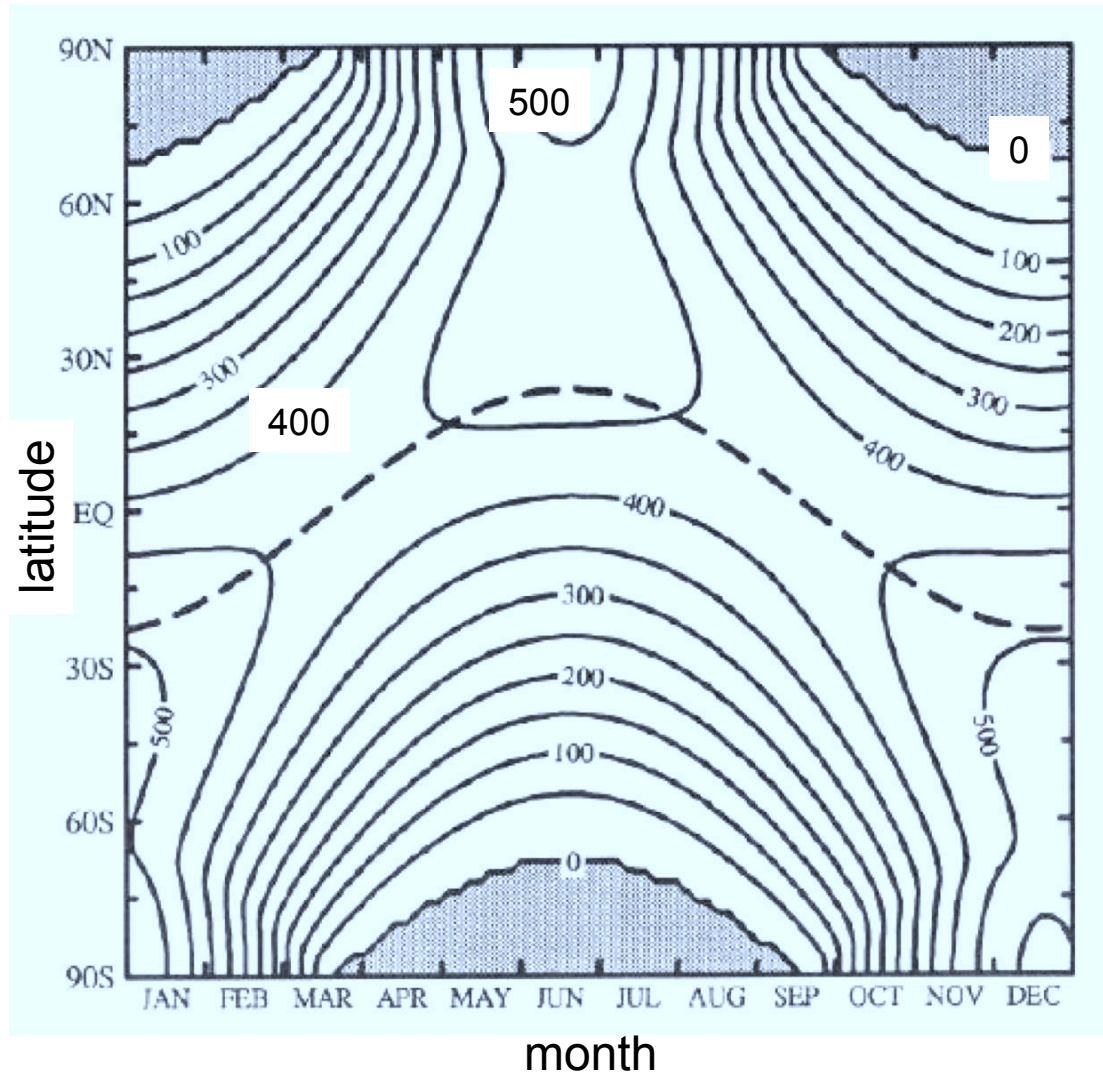
Longwave emitted  
to space, F

The difference:  
Drives climate dynamics  
to alleviate imbalances



## Daily mean insolation at top of atmosphere

- peaks at poles at summer solstice.
- is zero at poles at winter solstice.
- global average  
~  $342 \text{ Wm}^{-2}$



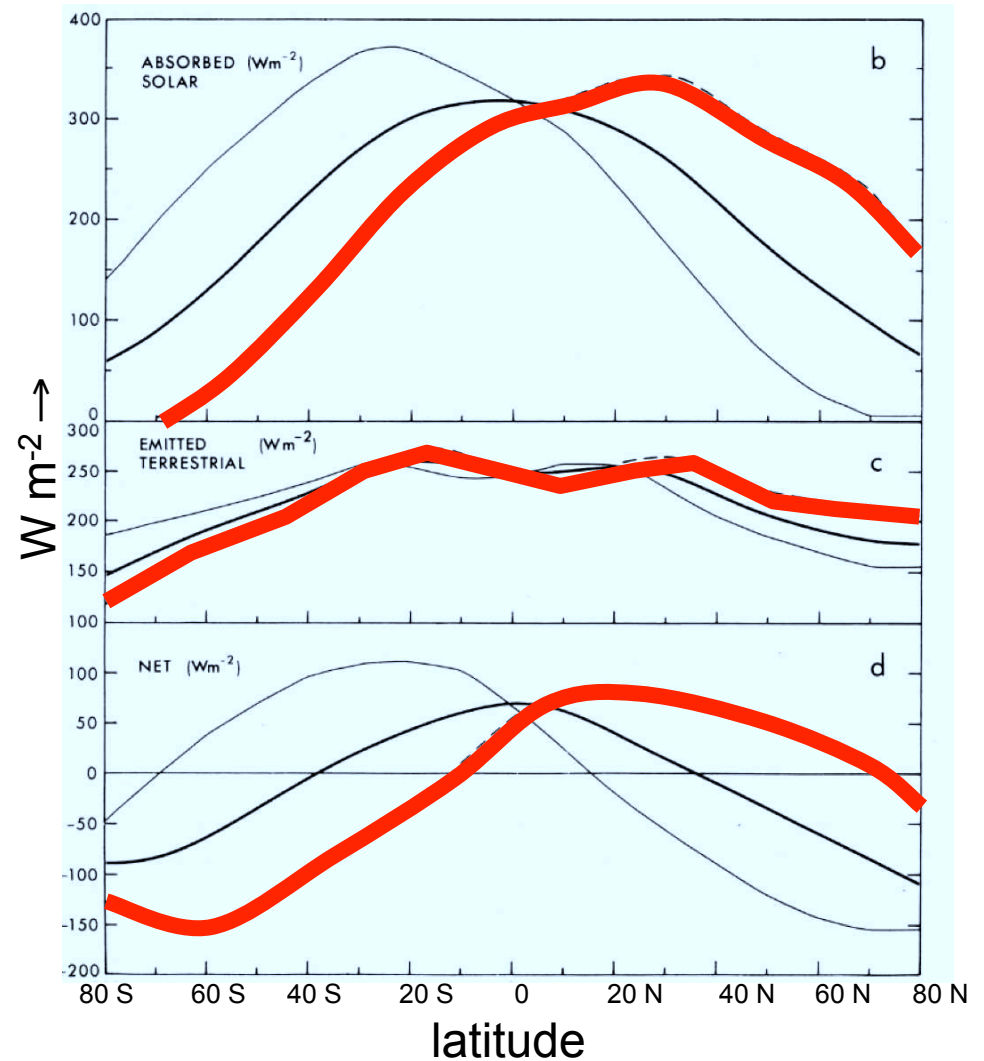
# Northern summer radiation budget (Jun. Jul. Aug.)

Absorbed solar

$Q_0(1-\alpha)$ :

Longwave  
emitted to space,  $F$ :

The difference: drives  
climate dynamics AND  
heat storage

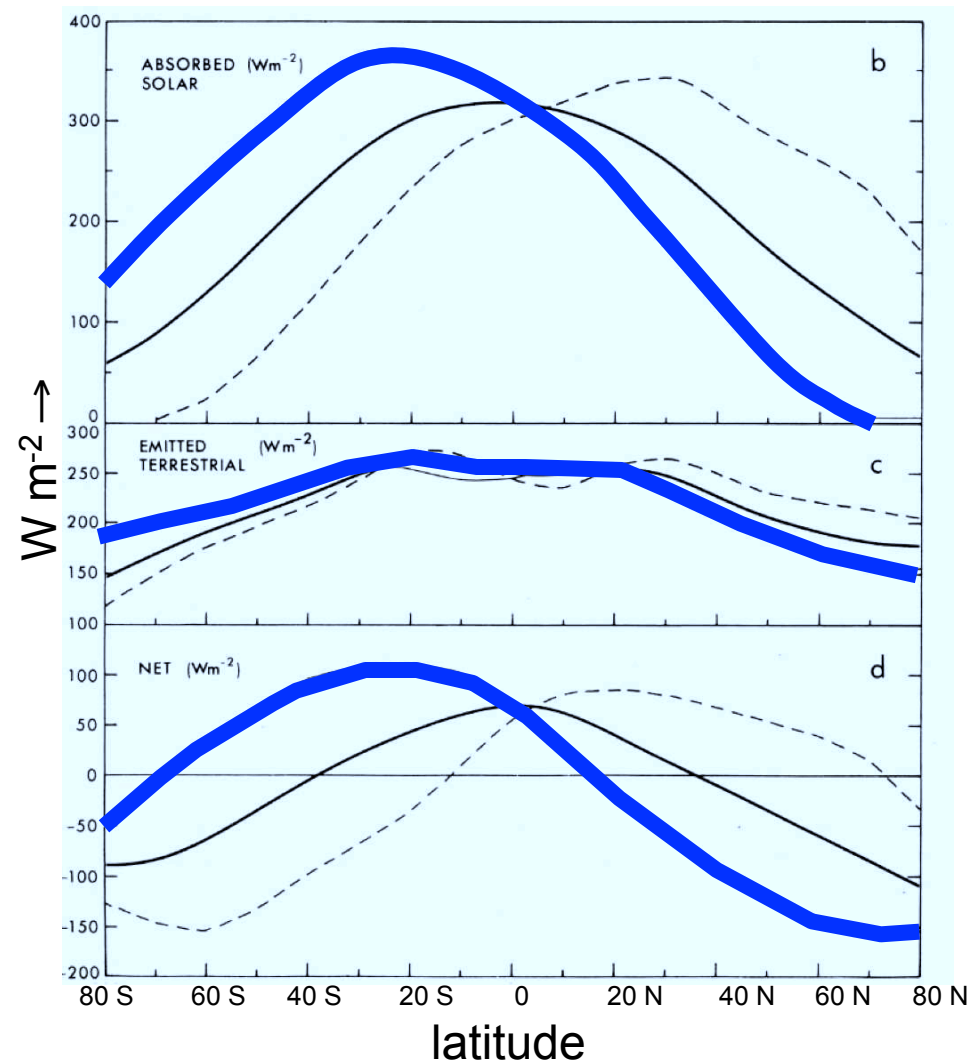


## Northern winter radiation budget (Dec. Jan. Feb.)

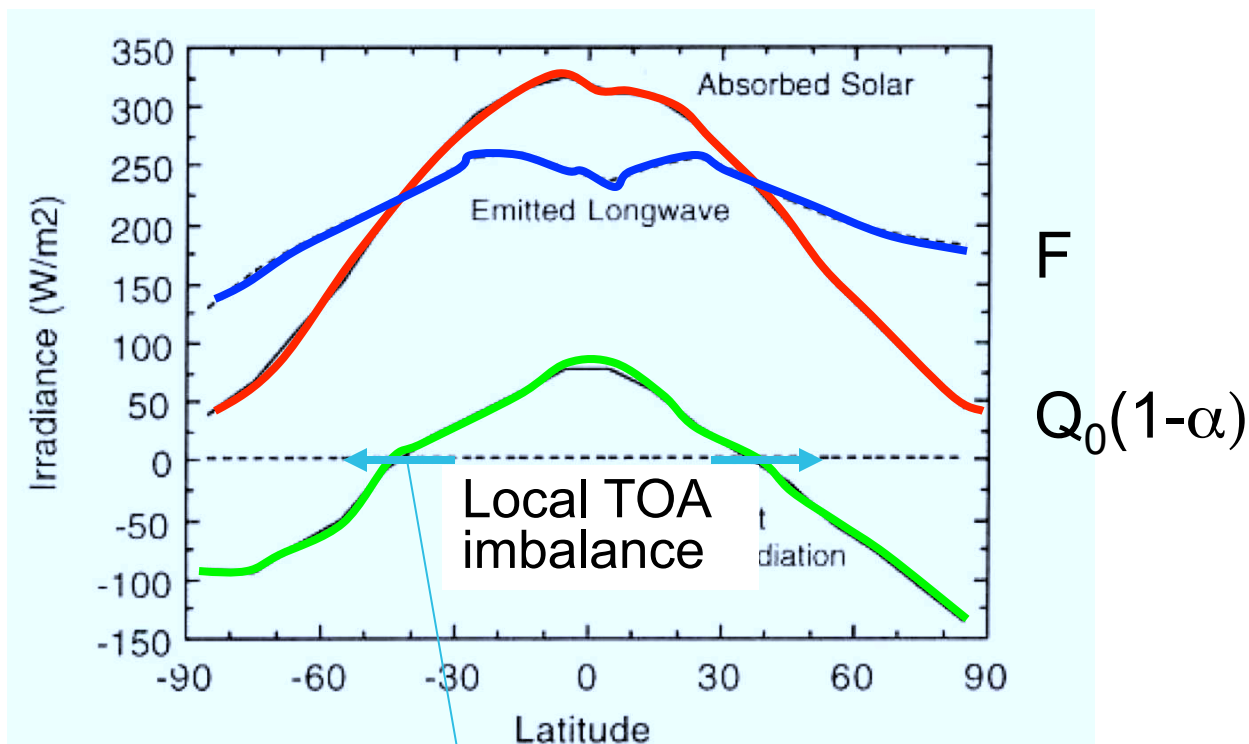
Absorbed Solar  
 $Q_0(1-\alpha)$ :

Longwave  
emitted to space,  $F$ :

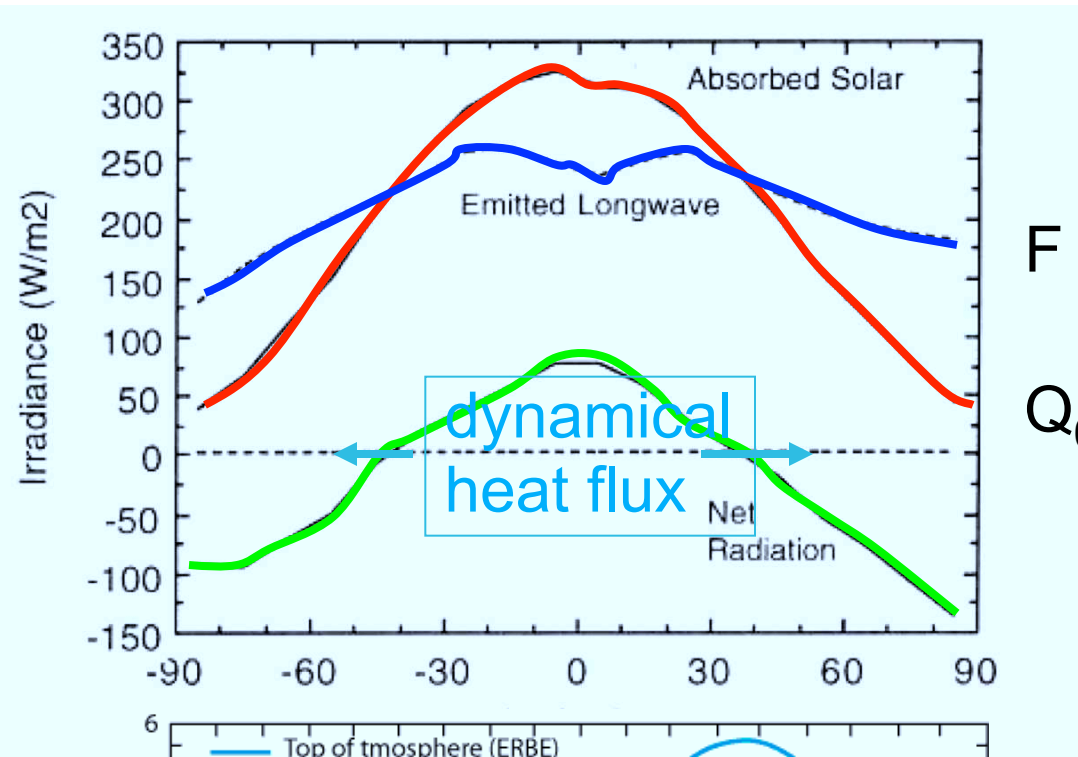
The difference: drives  
climate dynamics AND  
heat storage



# Top of Atmosphere (TOA) Flux Balance

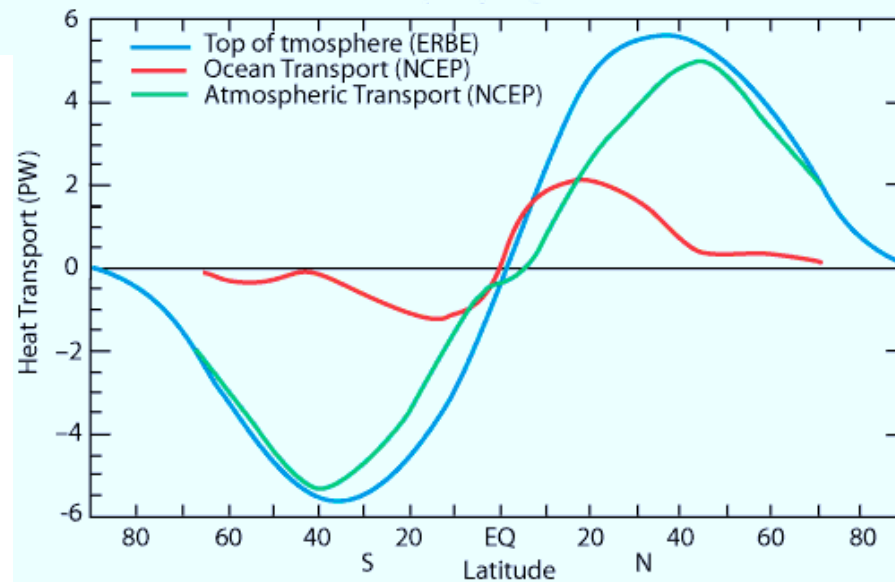


Local TOA imbalance drives dynamical heat flux such that the TOA imbalance is equal to the heat flux divergence. The imbalance is small relative to  $F$  or  $Q_0(1-\alpha)$  in most regions, except at the poles



$F$

$$Q_0(1-\alpha)$$



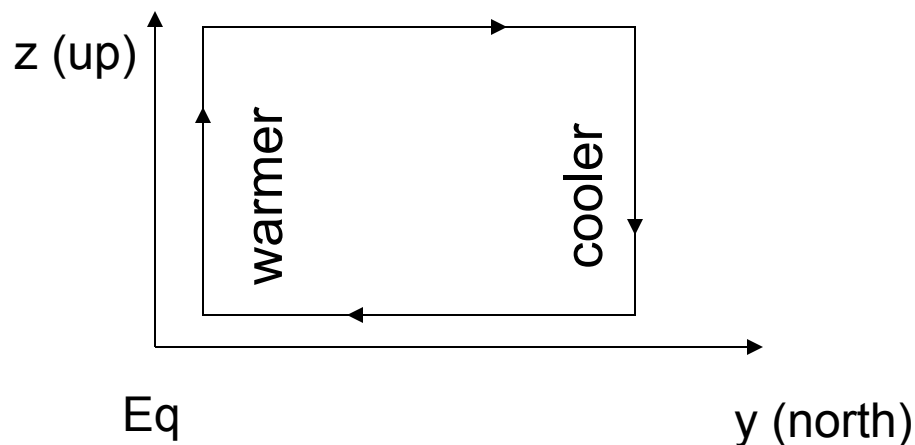
$H_T$  Gradient  
Seeks to  
Balance TOA  
Imbalance



# Atmospheric General Circulation in <15 minutes

Point 1: Temperature gradient develops owing to differential heating

## Hadley Circulation



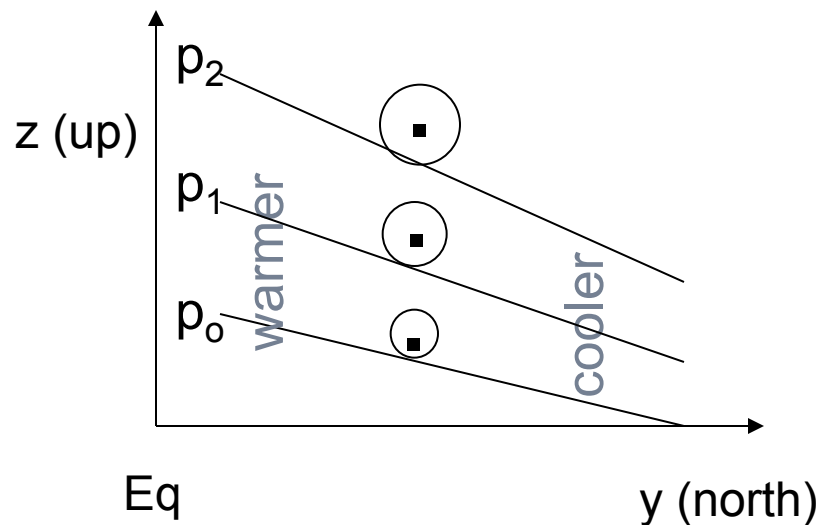
- “Thermally direct” meridional cell
  - Warmer air rises in the tropics (cooling it somewhat).
  - Cooler air sinks further north (warming it somewhat)
- Cooler air moves equatorward at surface
- Heat transport is primarily via potential energy

Point 2: Temperature gradient drives thermally direct cell, which moves heat poleward

Point 3: Temperature gradients cause vertical shear of the horizontal wind (see intro meteorology text book)

$$\frac{\partial u}{\partial z} \sim \frac{\partial T}{\partial y}$$

u = westerly wind  
T = temperature  
z = up in atm, ? in ocn  
y = north  
x = east

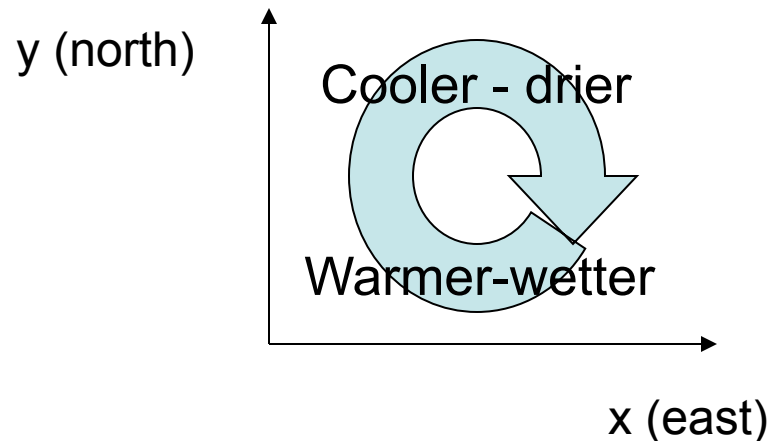


- Isobar slope increases with height
- Isobar slope determines geostrophic wind speed
- Westerly wind speed increases with height

◻ = Westerly wind

Vertical shear of horizontal wind is baroclinically unstable  
- encourages storm production, which limits the poleward reach of the Hadley Circulation to about 30 deg latitude

## Midlatitude Baroclinic Eddies (aka Storms)



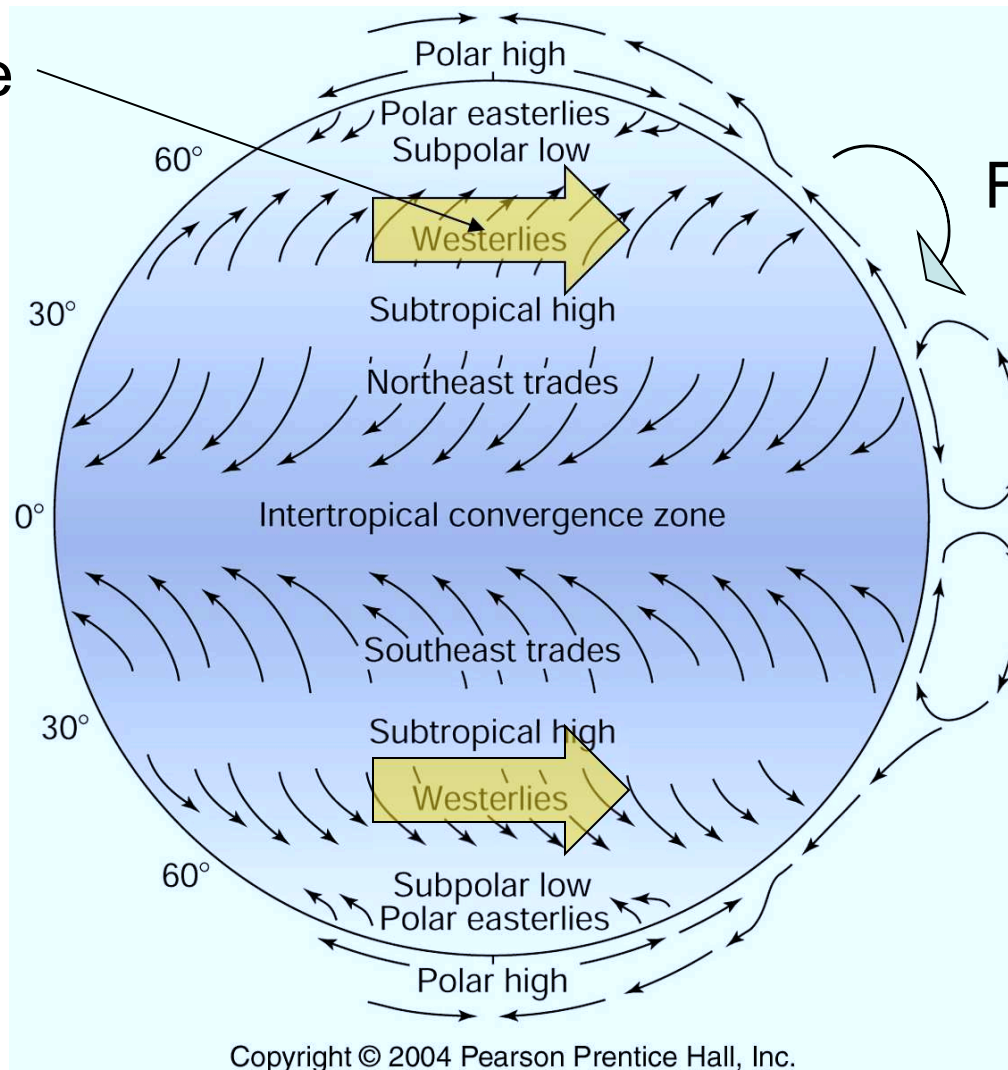
- Eddies arise owing to horizontal temperature gradient
- Eddies transport heat towards the pole
- Eddies erode north-south temperature gradient and hence weaken their energy source

Point 4: Horizontal eddies move heat poleward and incidently produce a thermally **indirect** meridional cell known as the Ferrel cell (see intermediate meteorology text)

# Ocean Circulation in <15 min

## Surface Winds (crudely)

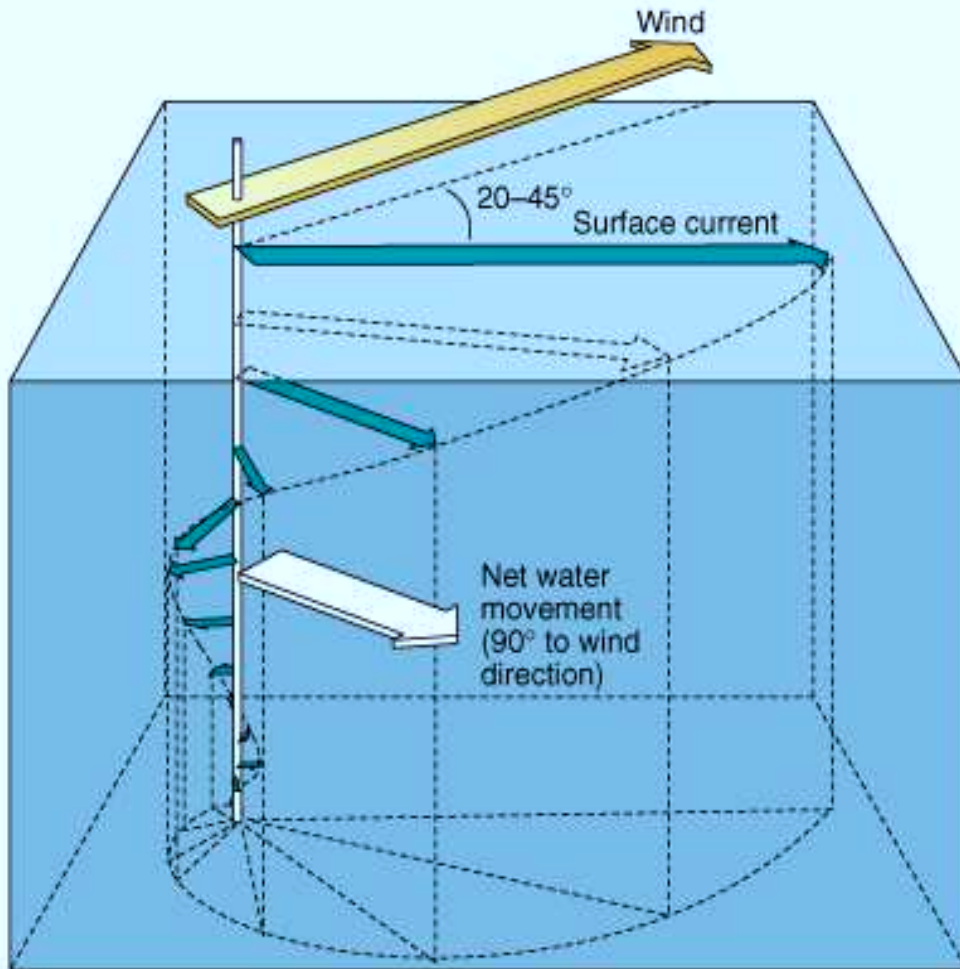
Midlatitude  
westerlies  
aloft



Ferrel Cell

Hadley Cell

## Ekman drift (in the NH)

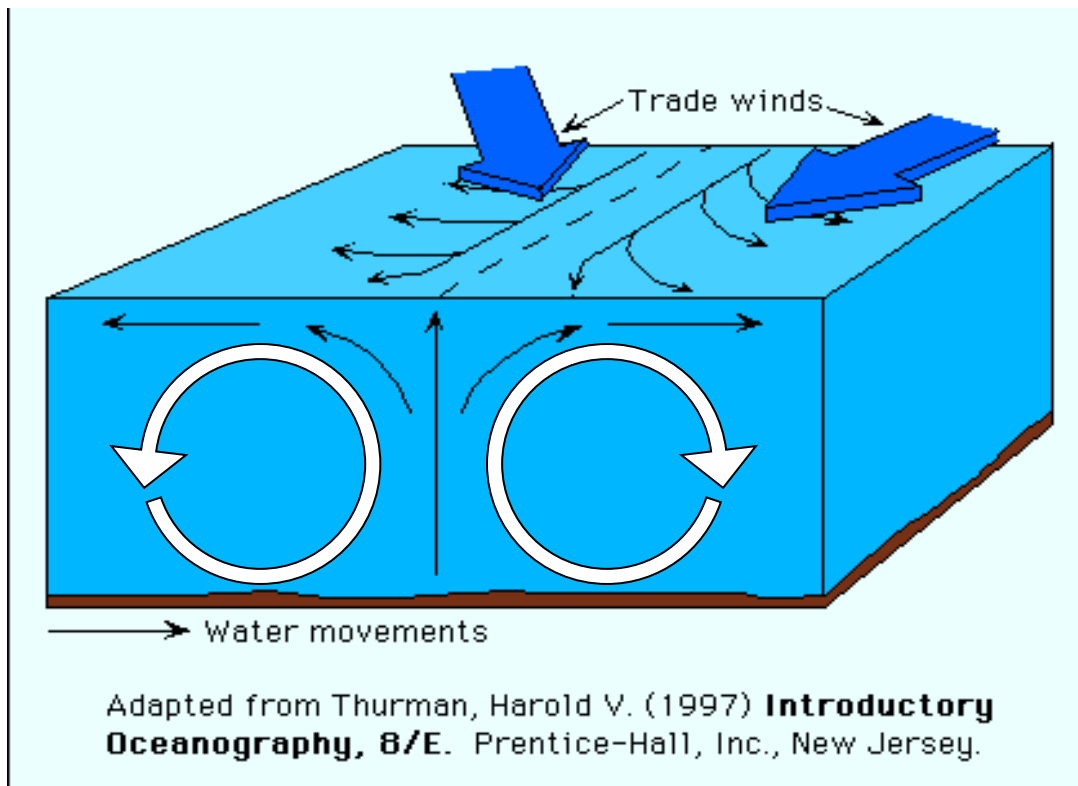


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- Wind drags surface and friction drags layers beneath
- Deflected to the right by Coriolis Force
- Results in spiraling pattern
- Net transport of water to the right of the wind.

Nansen's student Ekman solved this after Nansen saw icebergs moving at right angles to the wind

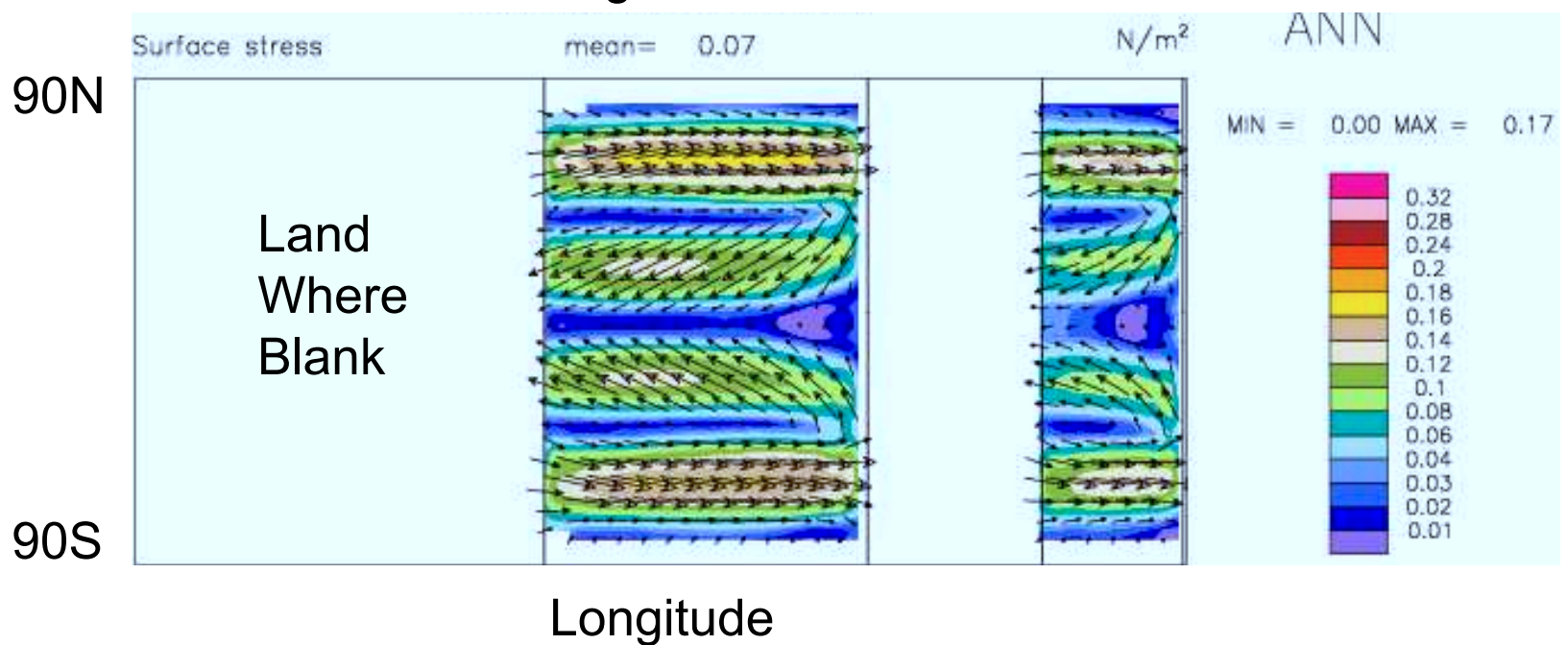
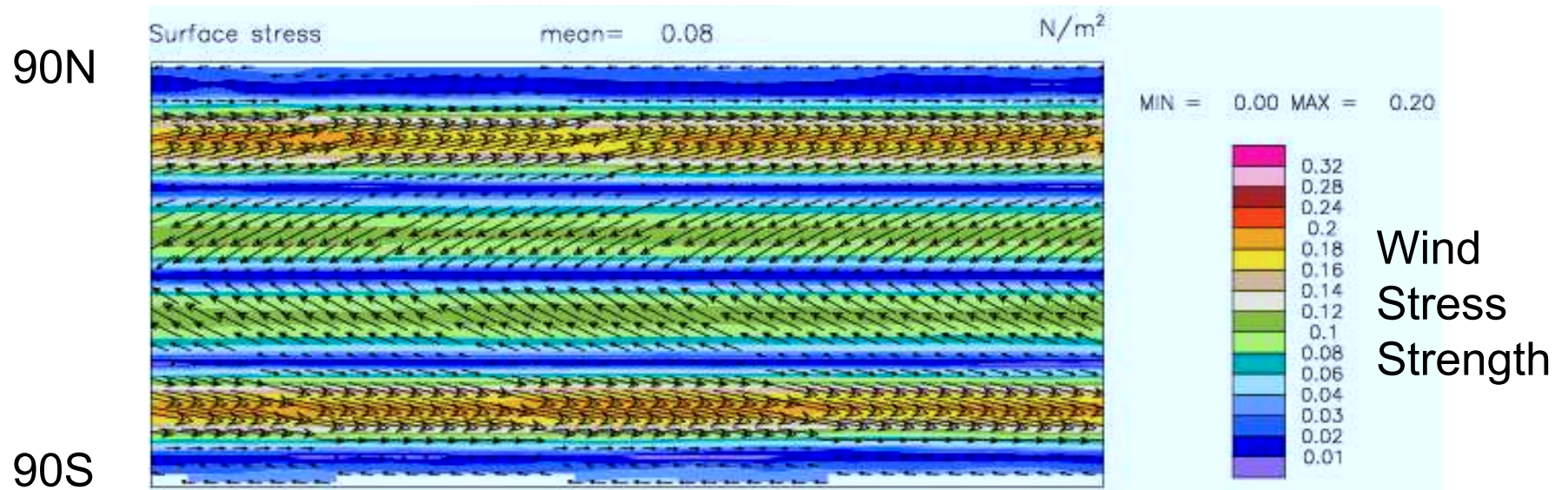
# Equatorial Upwelling

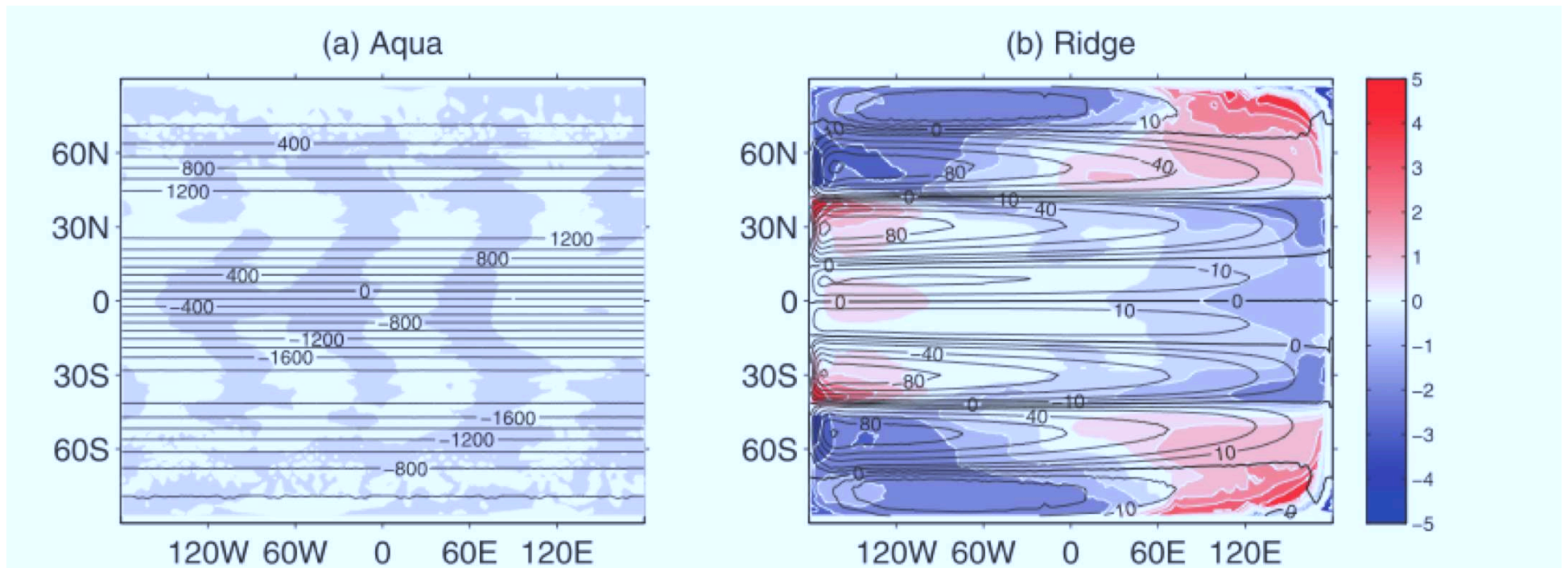


- Trade winds blow surface toward the west
- Ekman flow transports water poleward in both hemispheres
- Upwelling cold water fills gap
- Causes a meridional circulation that moves heat poleward, “Eulerian mean”



# Wind variations cause gyres provided there is land





Sverdrupian gyre circulation on right only

Enderton and Marshall, 2009  
Figure 9



## Sverdrup Balance

$$M_y \approx -\frac{1}{\beta} \frac{\partial T_x}{\partial y}$$

$$\frac{\partial M_x}{\partial x} + \frac{\partial M_y}{\partial y} = 0$$

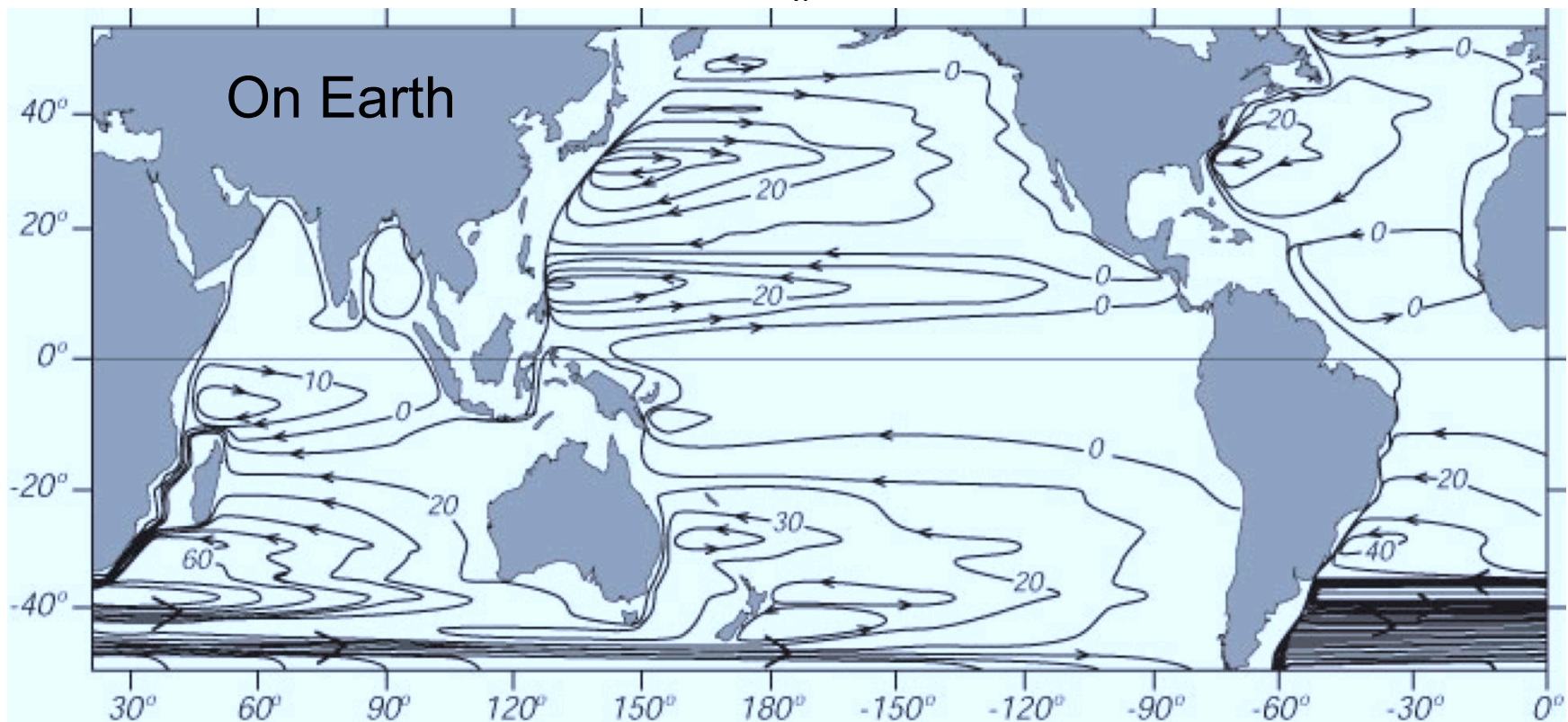
M = vertically integrated mass transport

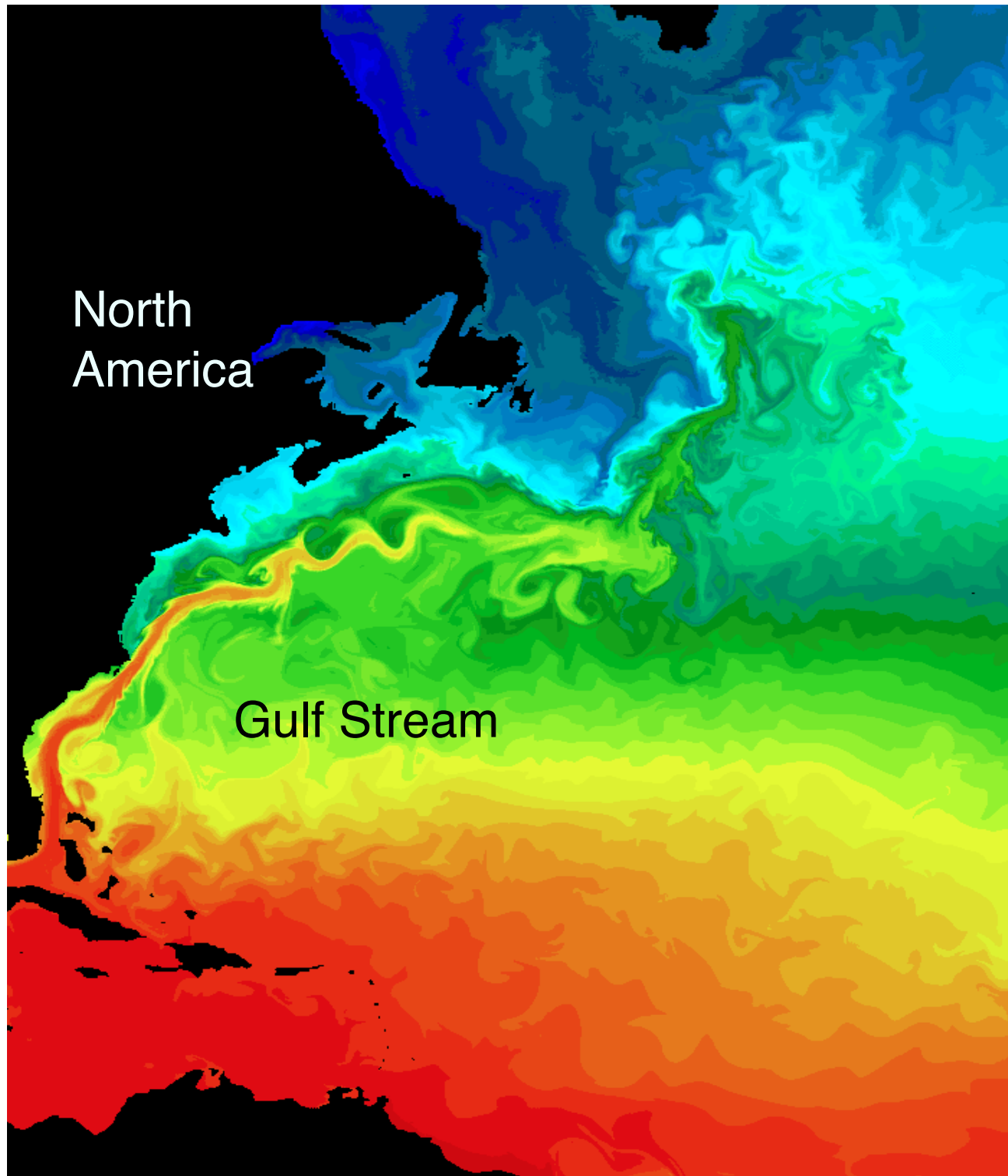
T = wind stress

$\beta = \partial f / \partial y$  is the rate of change of Coriolis parameter with latitude

recall x=east, y=north

Requires Boundary Condition  $M_x = 0$  at eastern boundary





North  
America

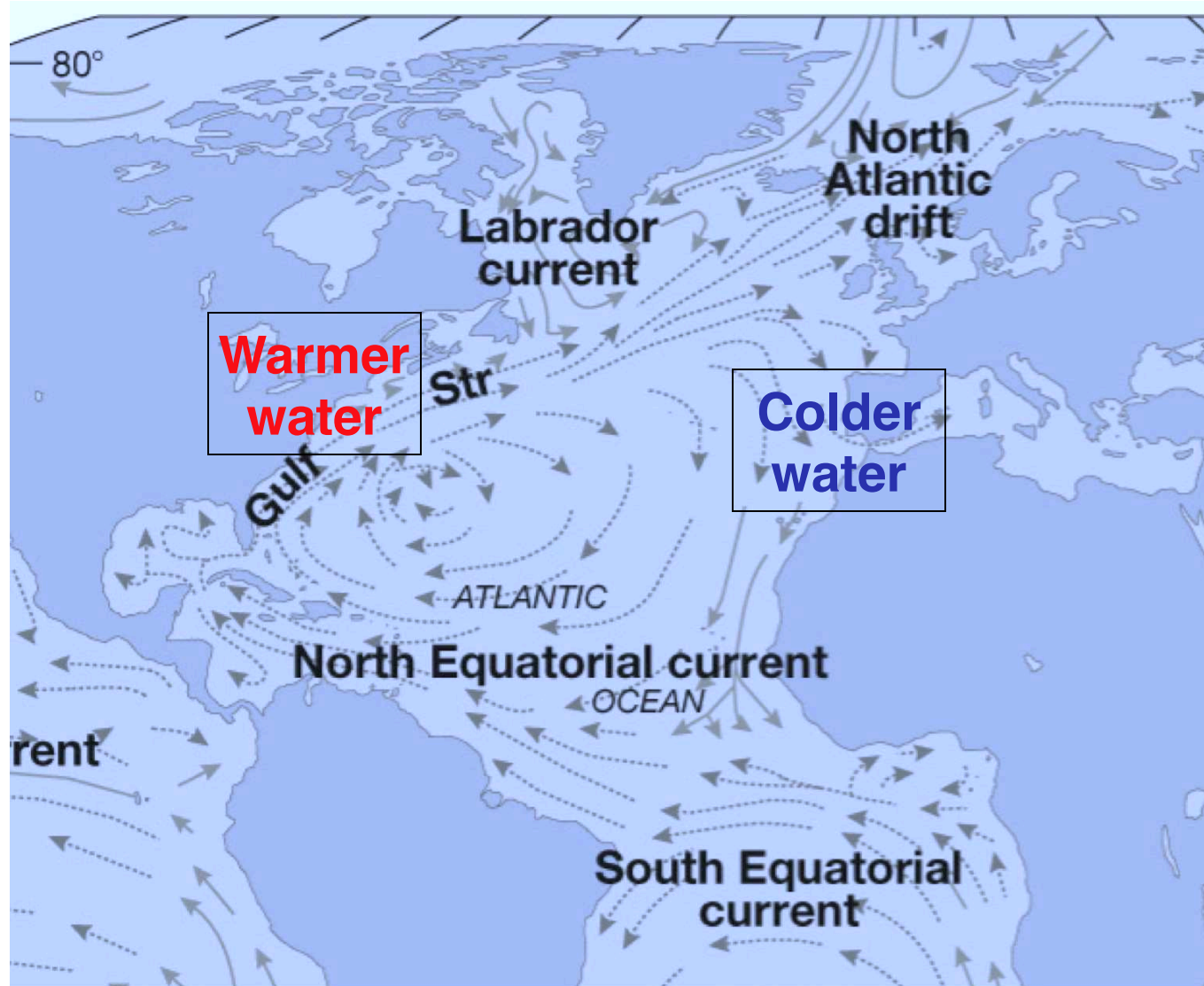
Gulf Stream

Gyres transport  
heat

Colors show  
Temperature

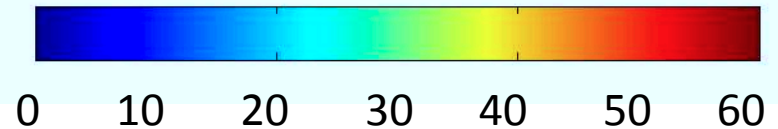
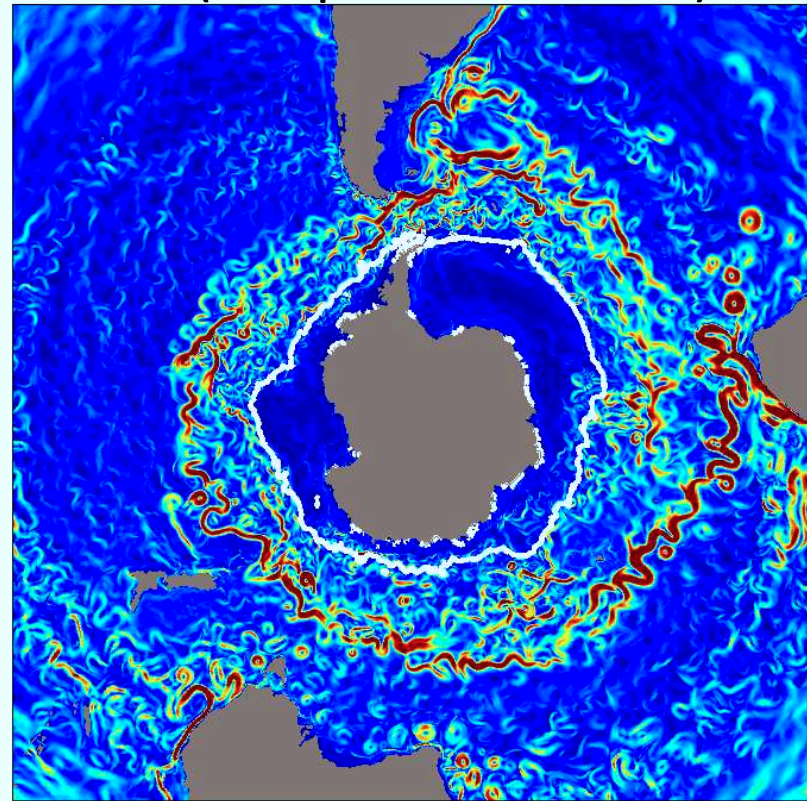
AVHRR satellite

**Gyres move heat and also cause meridional flow (Sverdrup Balance)**



Eddies move heat  
like mini-gyres

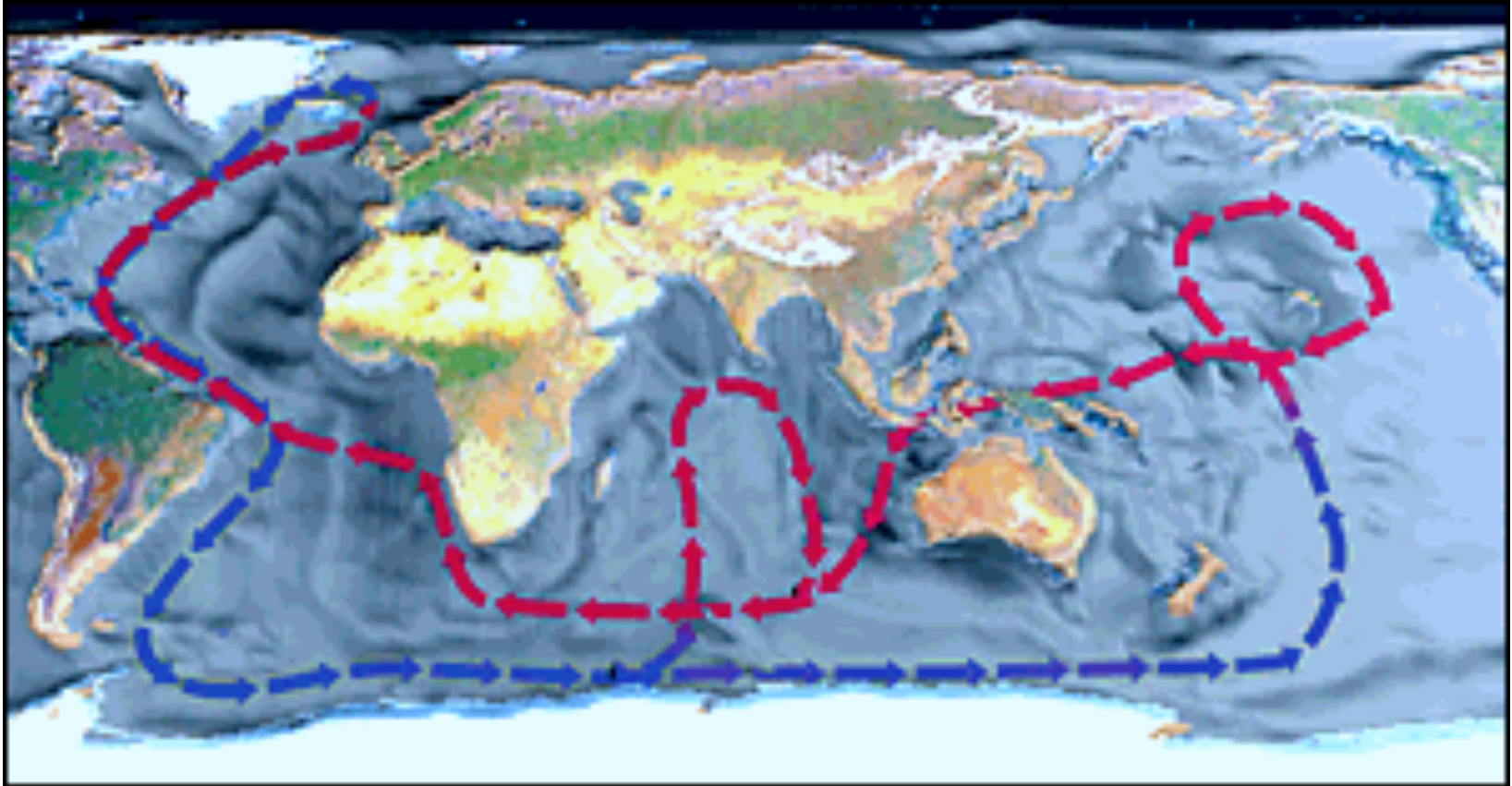
0.1° Simulation  
resolved (not parameterized) eddies



Current Speed in cm/s for randomly chosen October



Mean Meridional Circulation also moves heat



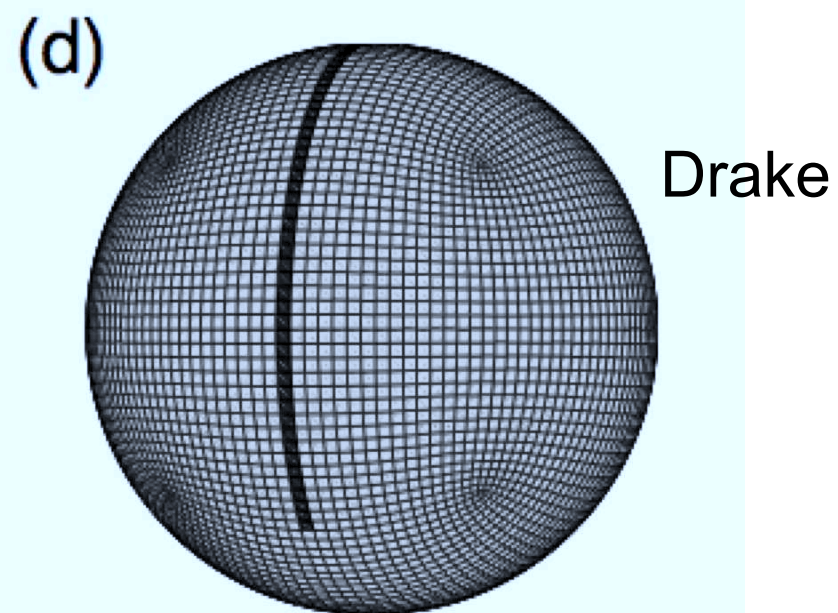
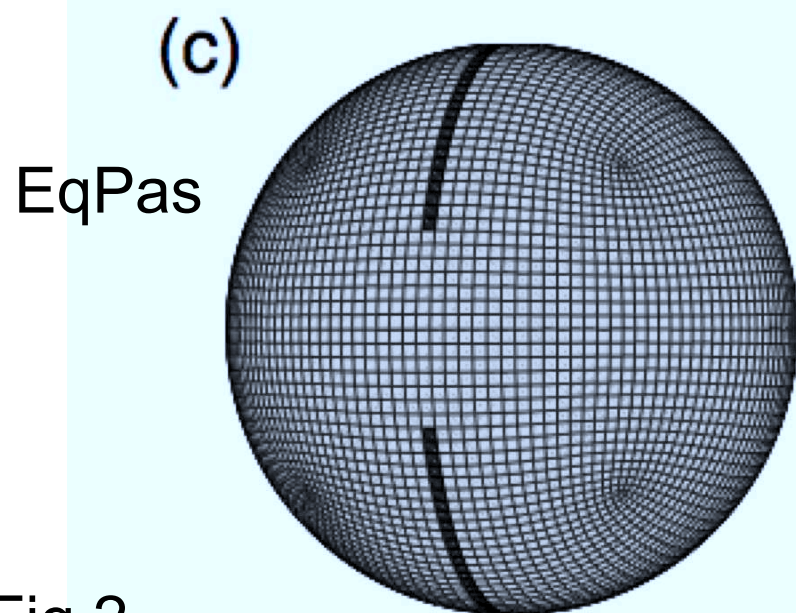
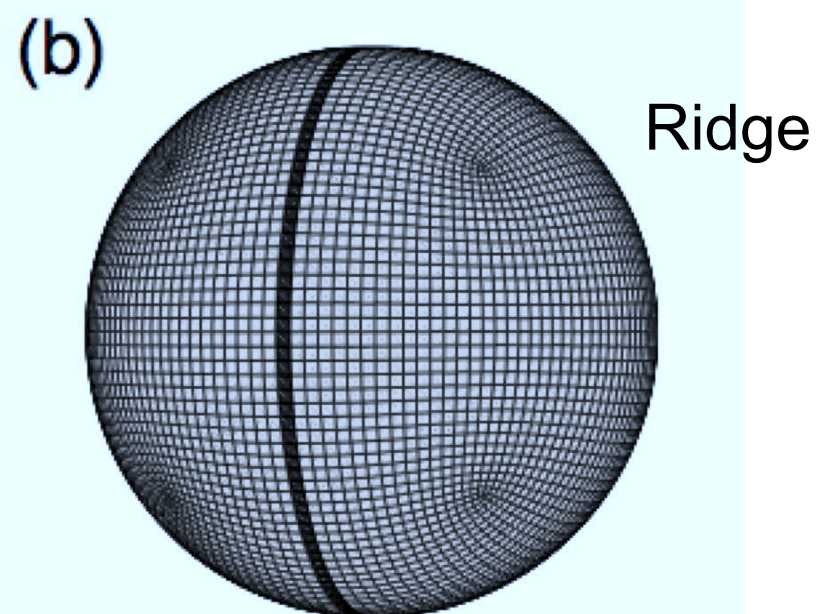
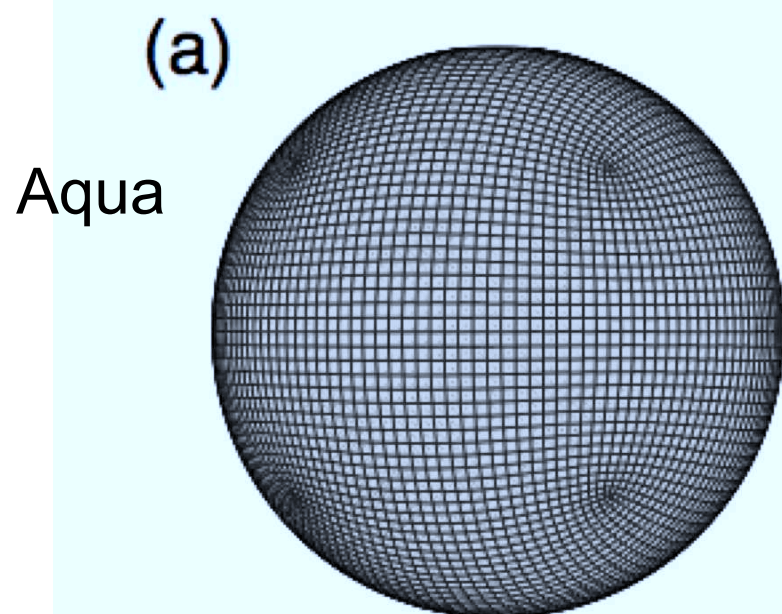


Fig 2

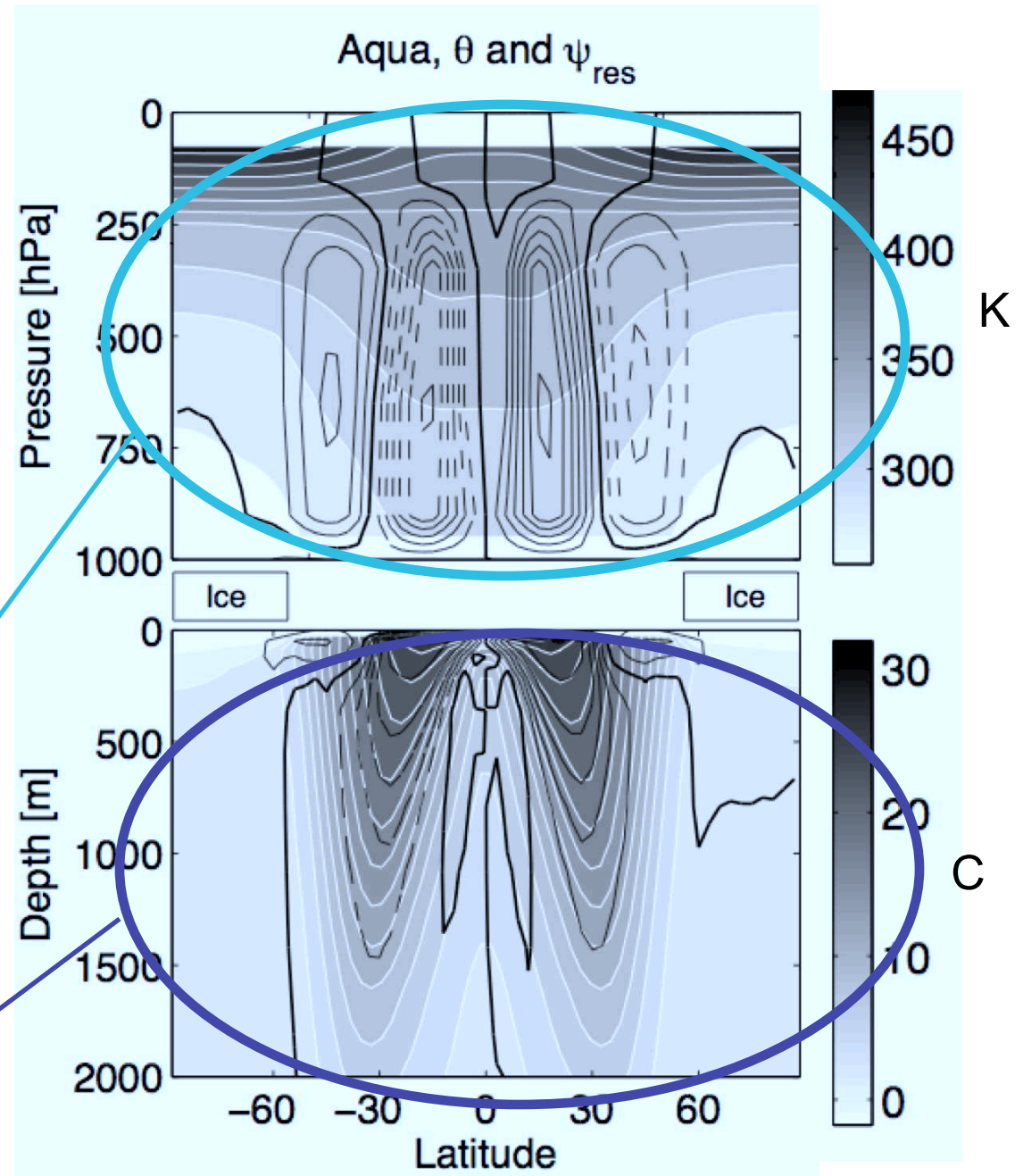


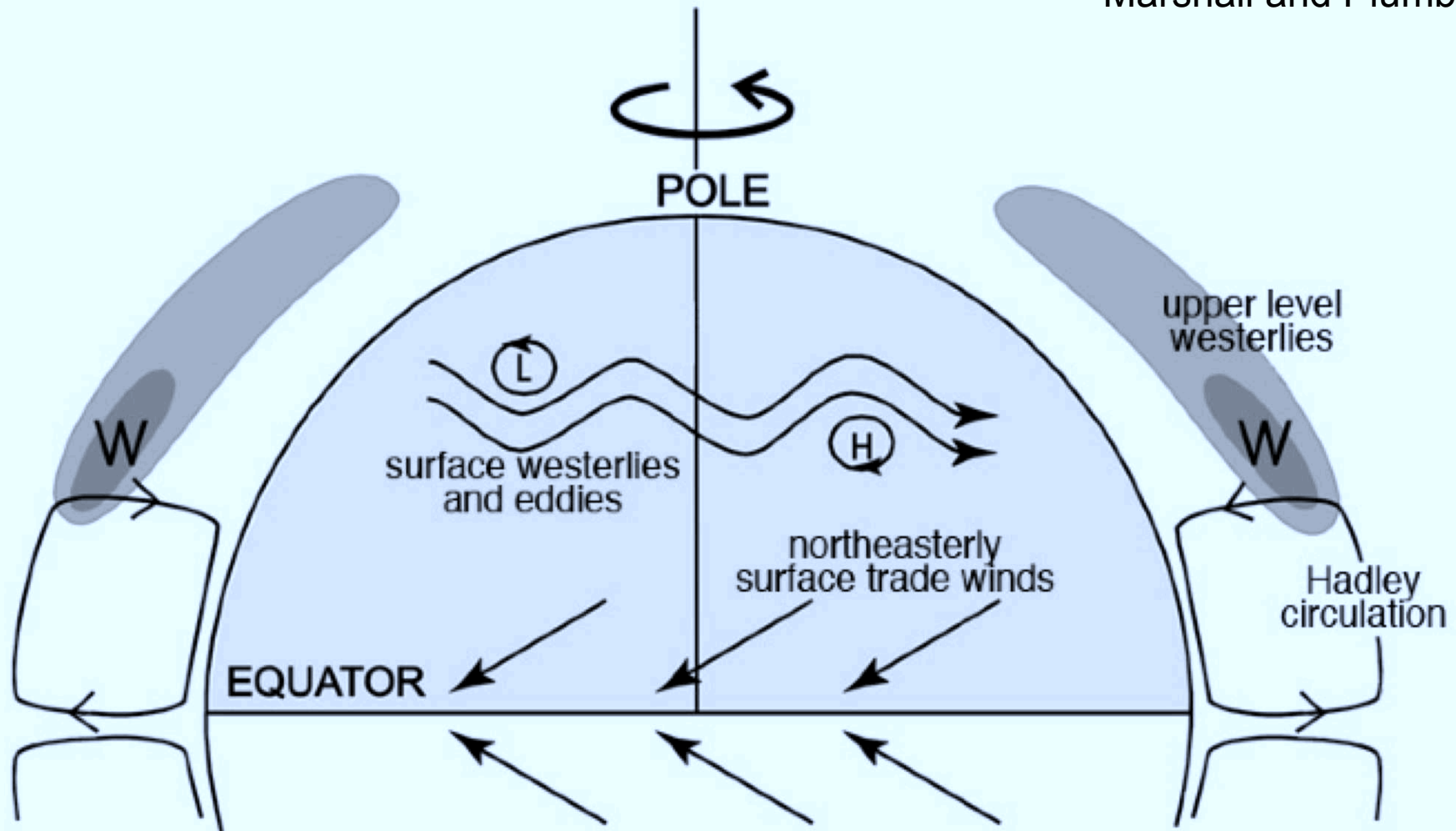
$\theta$  - Potential Temperature (shaded) temperature if air sinks adiabatically to surface, stratosphere has large  $\theta$  and is very stable

$\Psi_{\text{res}}$  - streamfunction (lines) denotes circulation

Atmosphere is in thermal wind balance, has Hadley and Ferrel Cells, strong midlatitude grad  $\theta$  and jets, etc

Ocean has sinking in the high latitudes and upwelling in the tropics. Little circulation under sea ice.

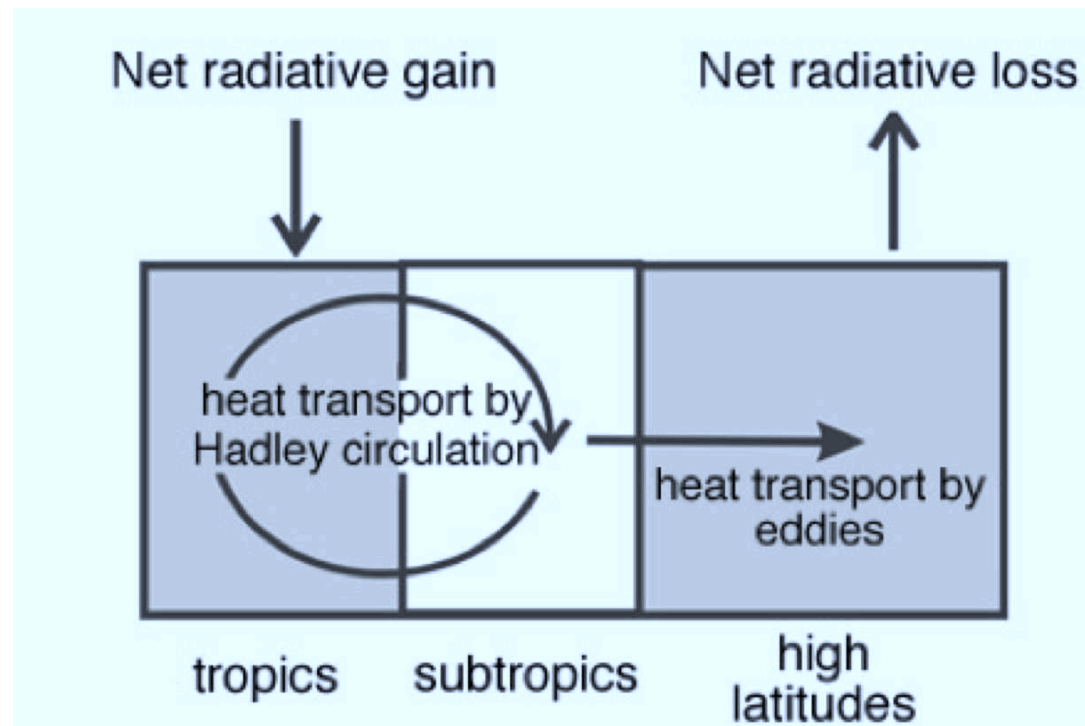




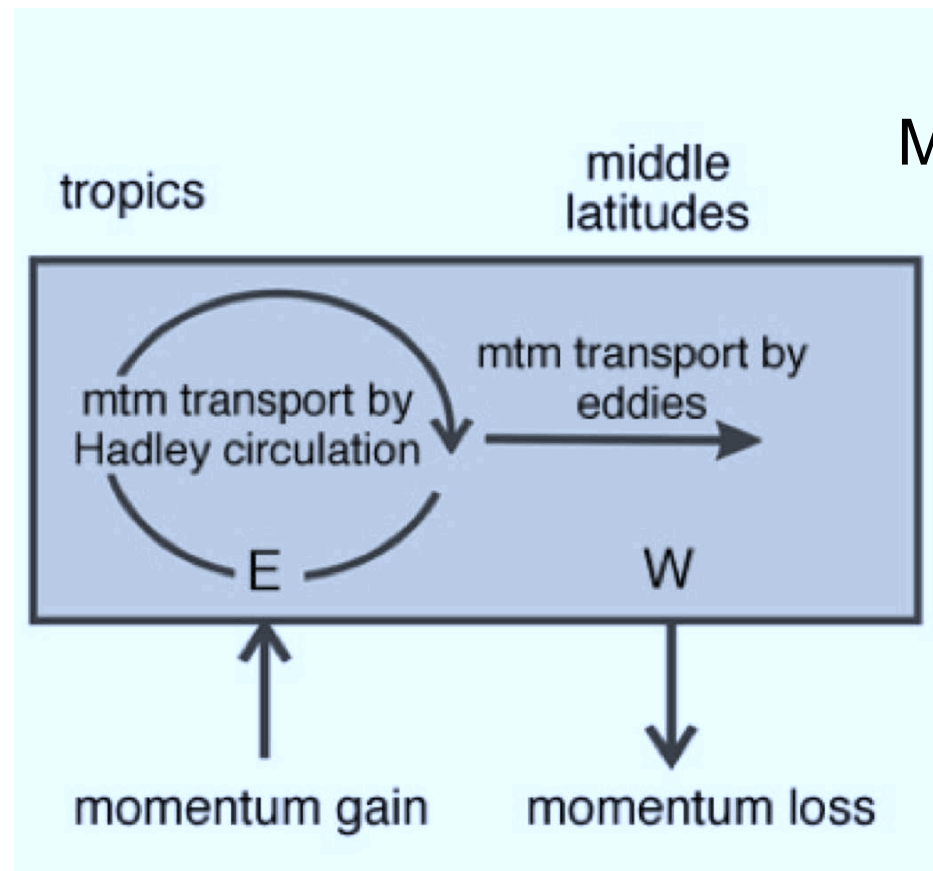
Ferrel cell in mid latitude (opposite sense of Hadley circ), results from momentum and heat budgets driven by eddies... see favorite meteorology text



## Marshall and Plumb



Weaker eddies also has implications for momentum transport



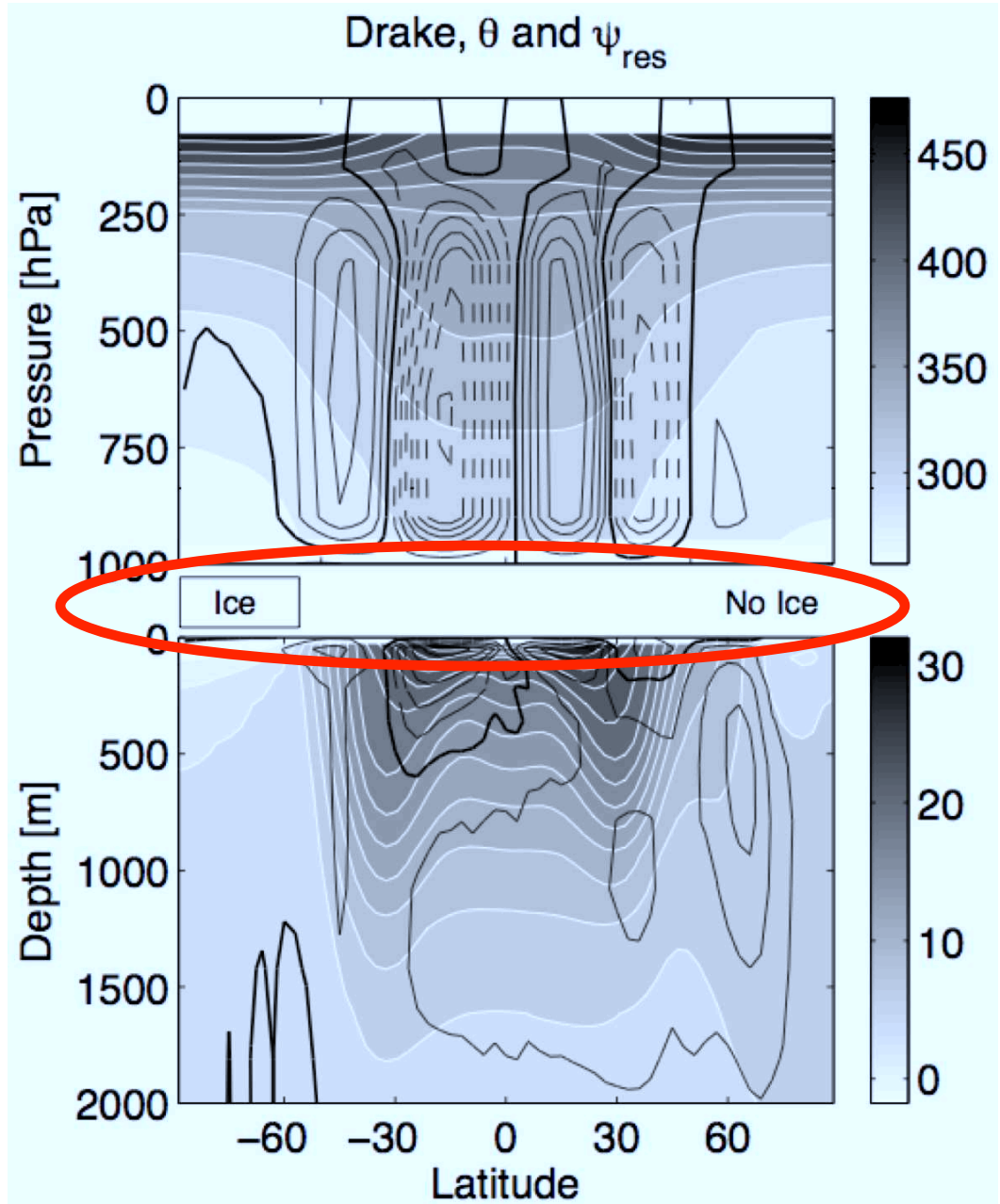
Marshall and Plumb

where winds are easterly

where winds are westerly

Wave dispersion causes shape of eddies to be non-circular in the horizontal such that they transport westerly momentum towards the pole, thus requiring easterlies in the tropics

Aqua had ice at both poles, but Drake only has ice at Drake passage pole



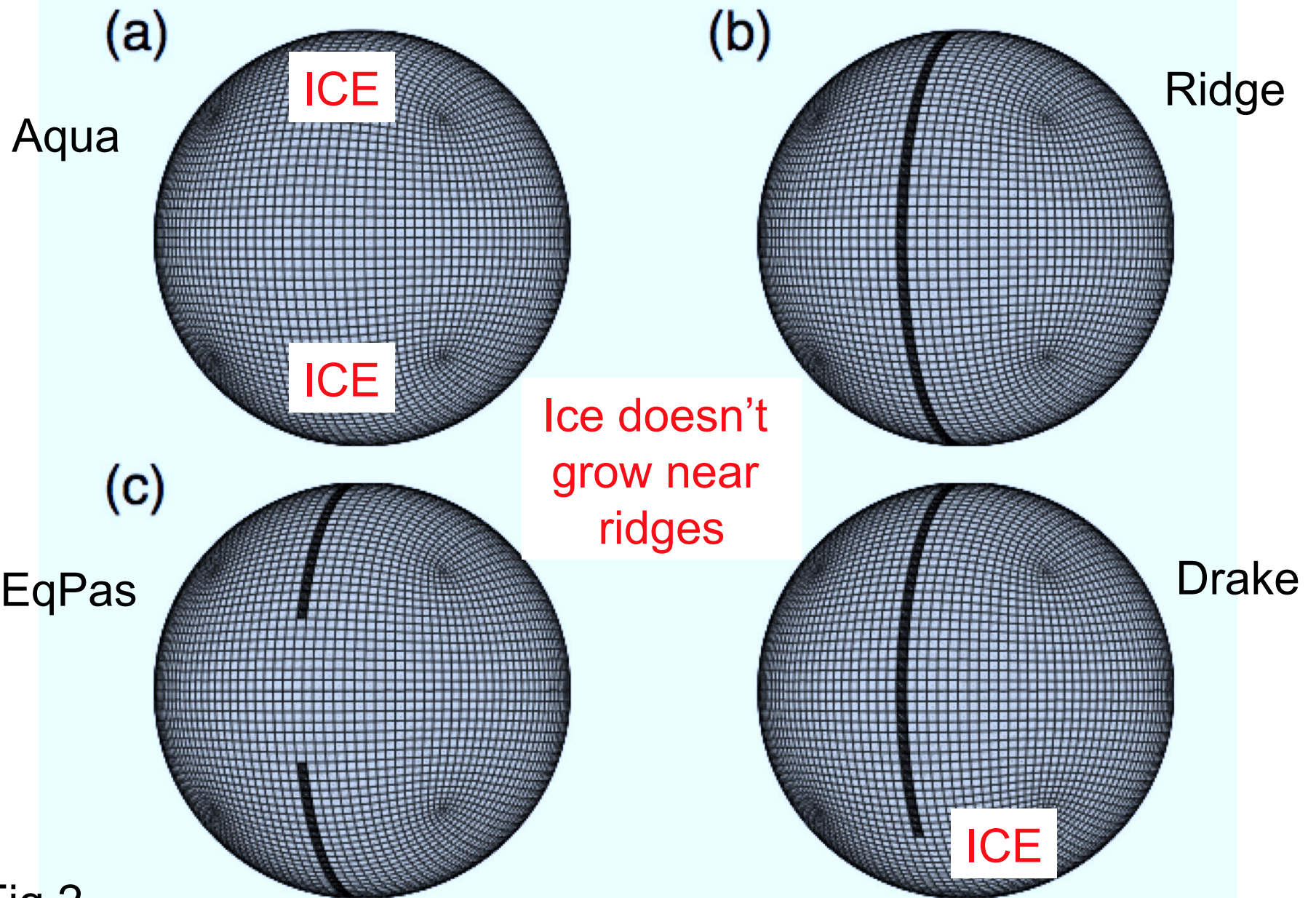


Fig 2



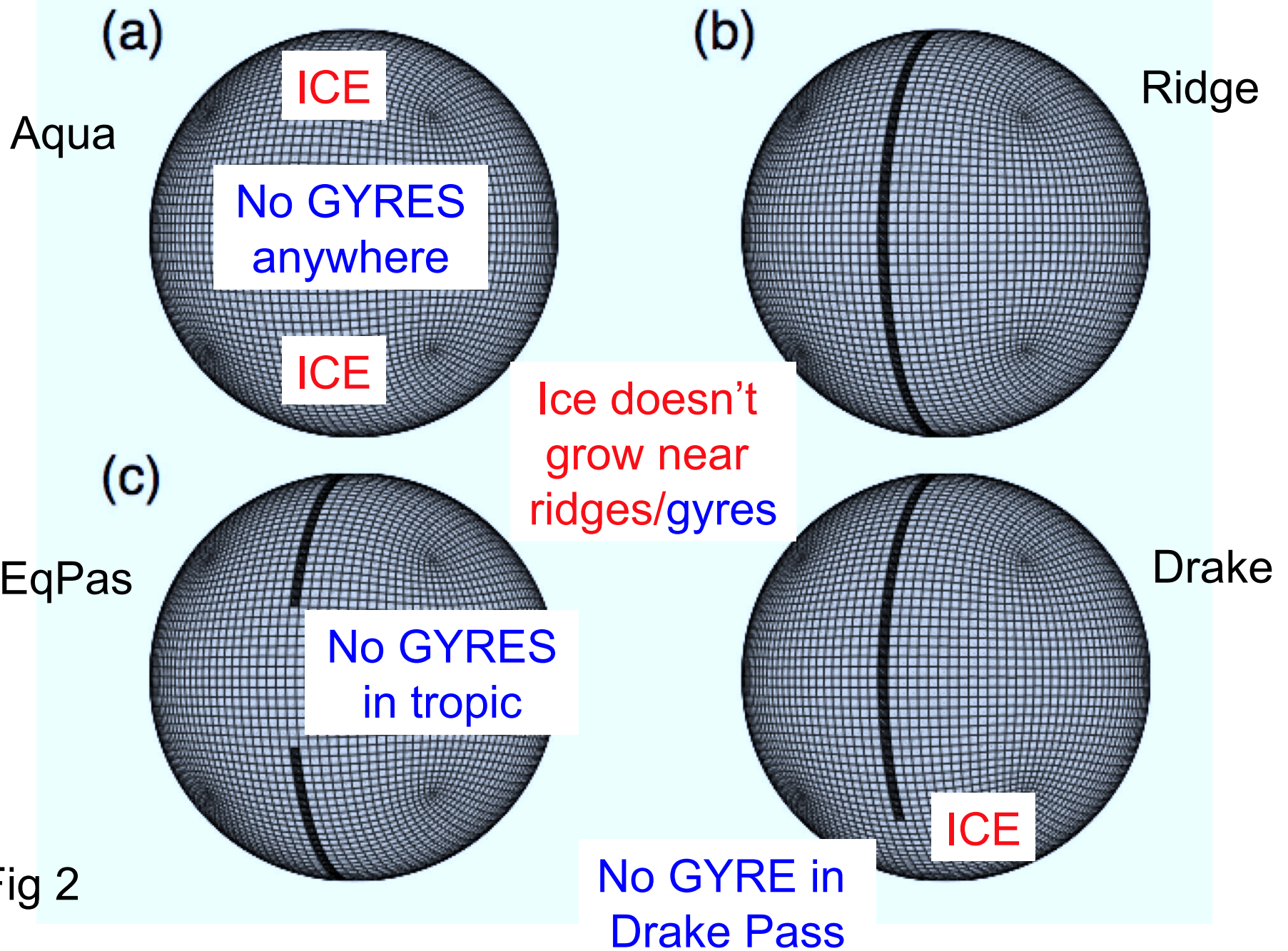
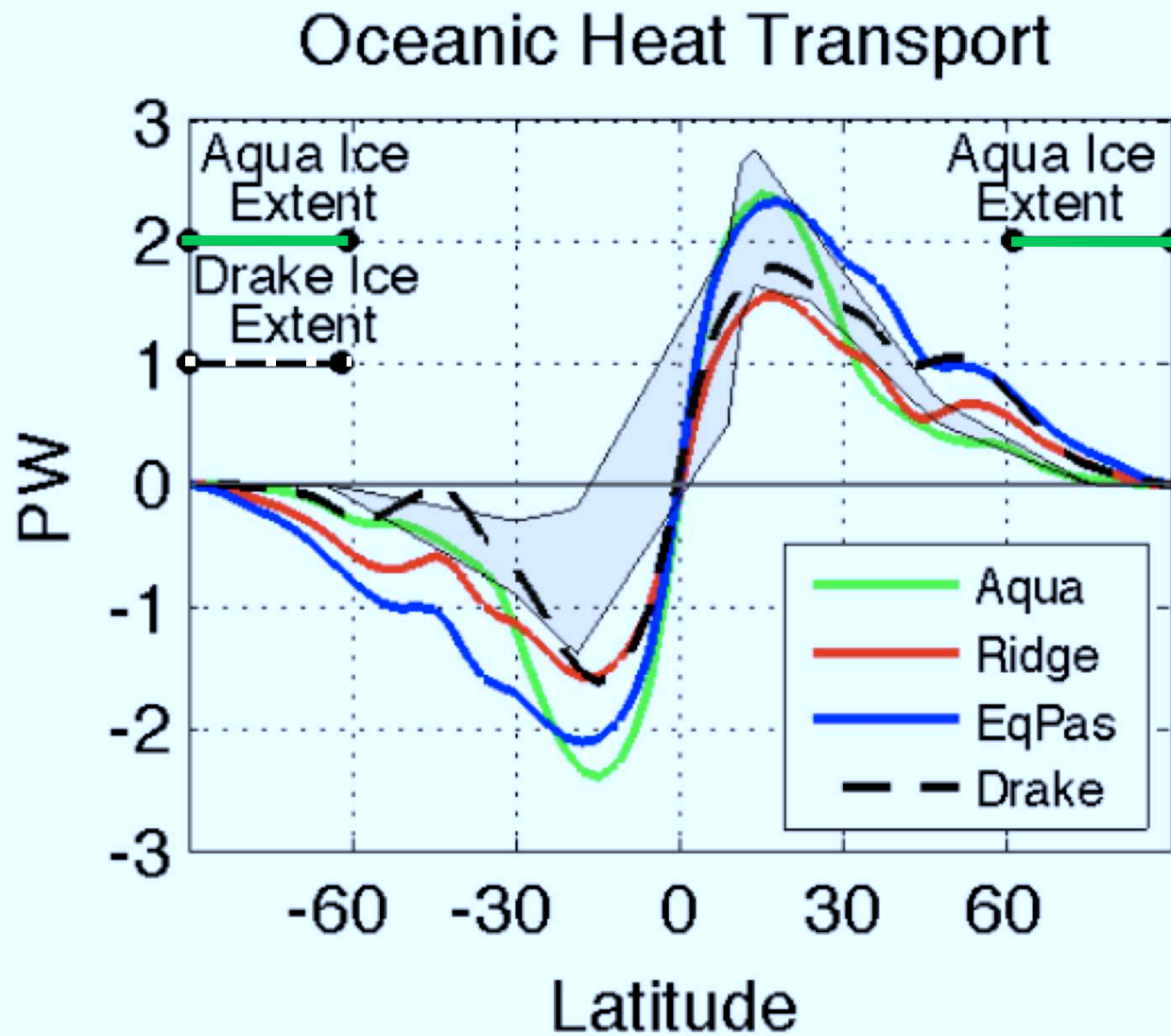
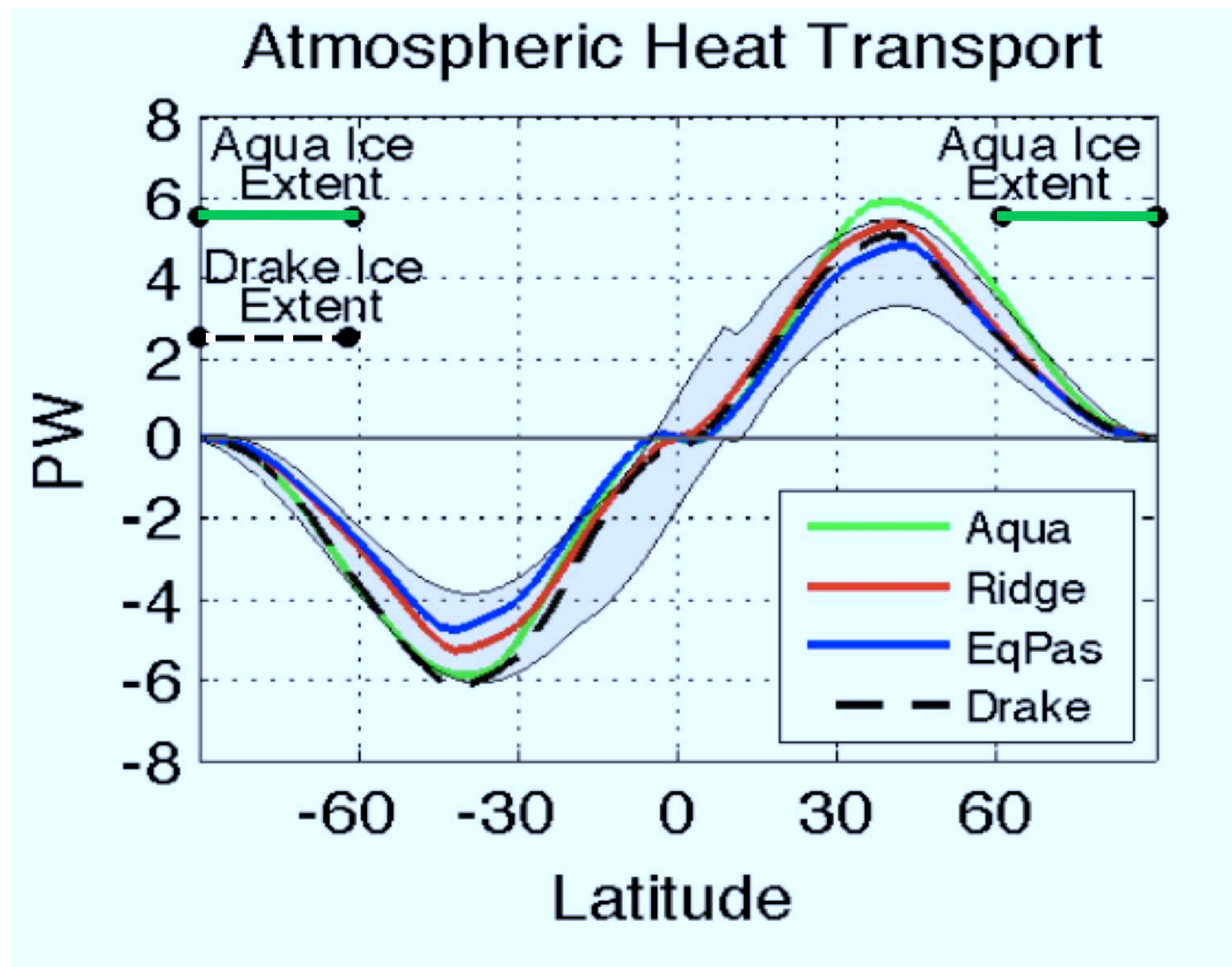


Fig 2

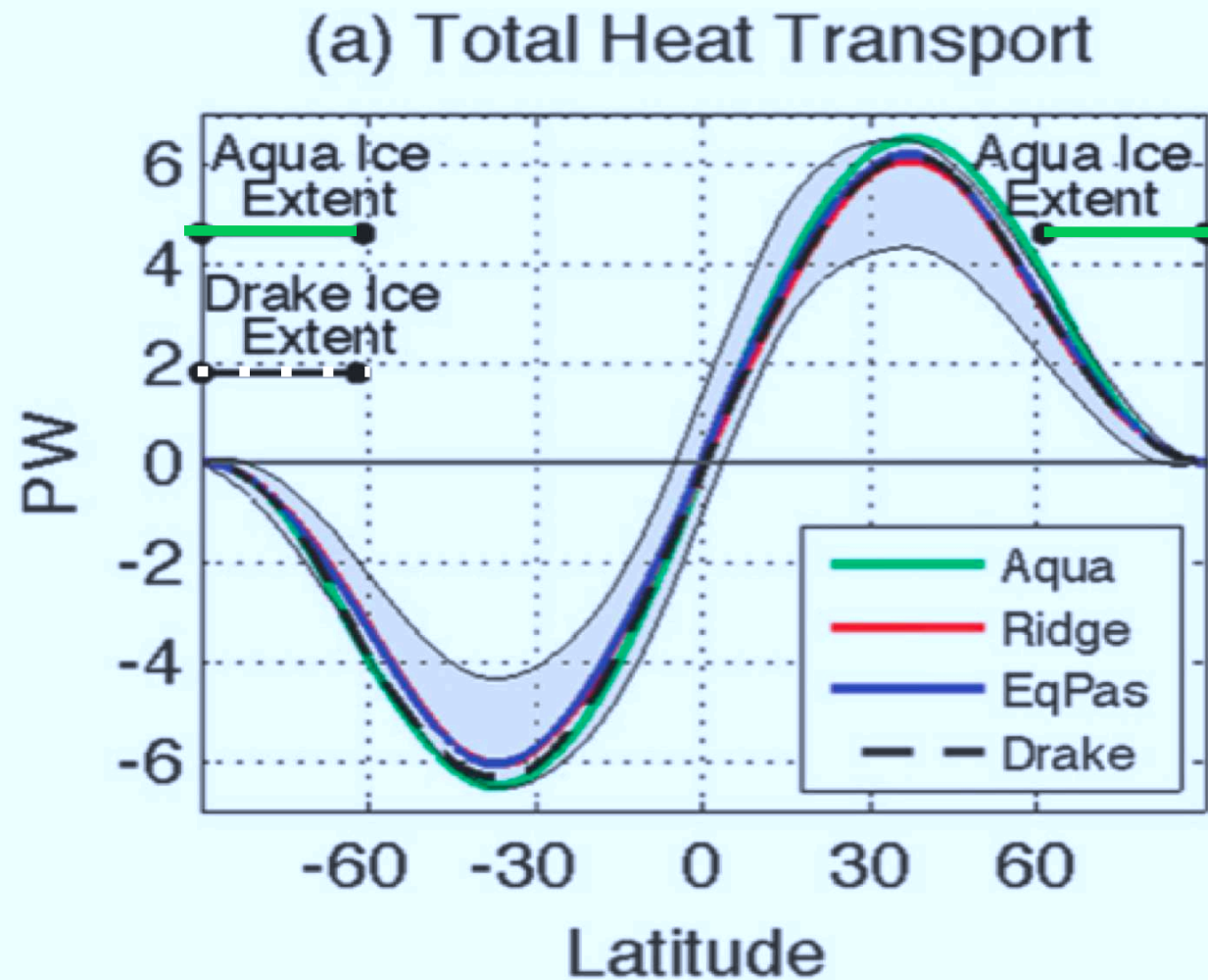
Without gyres, ocean heat transport at 60 N/S is inadequate to prevent ice



But atmospheric heat transport at 60 N/S over compensates

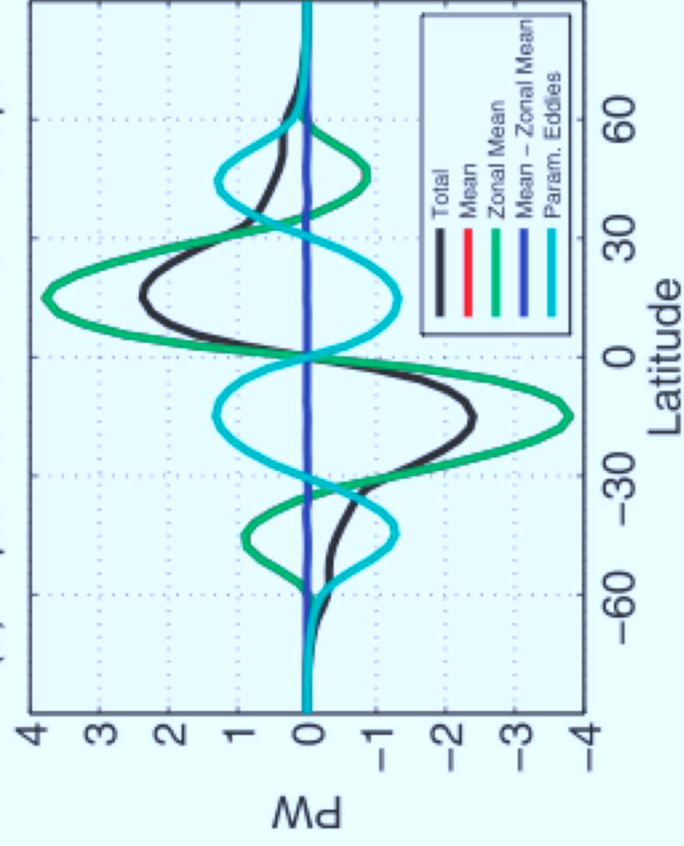


Ocean Heat Transport varies by X2 but total varies little

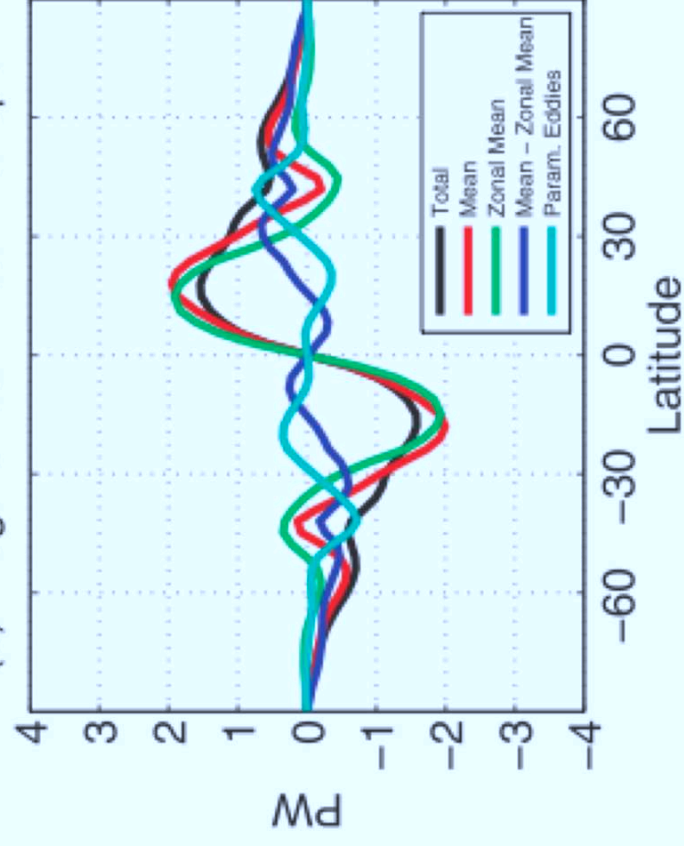




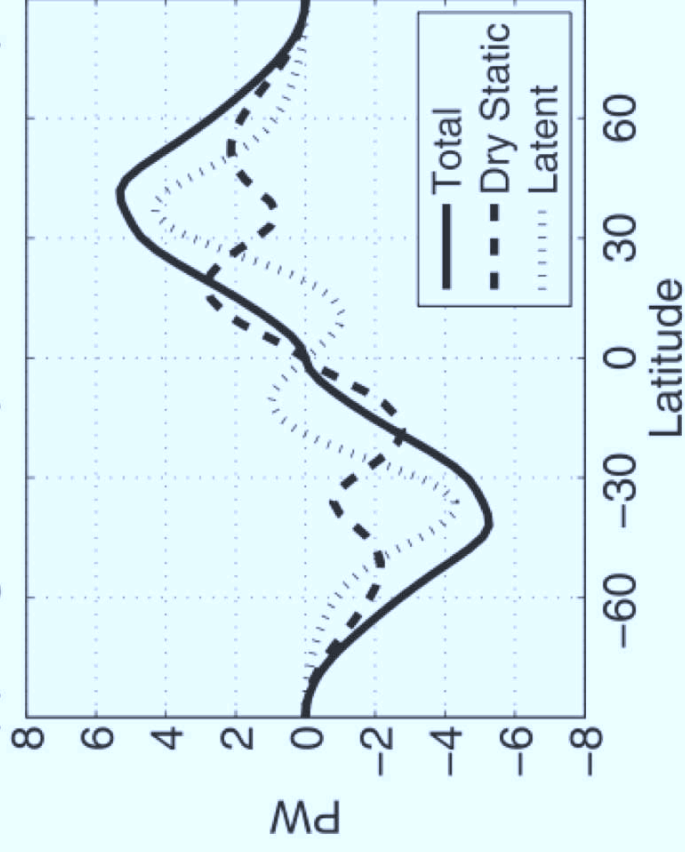
(a) Aqua Ocean Heat Transport



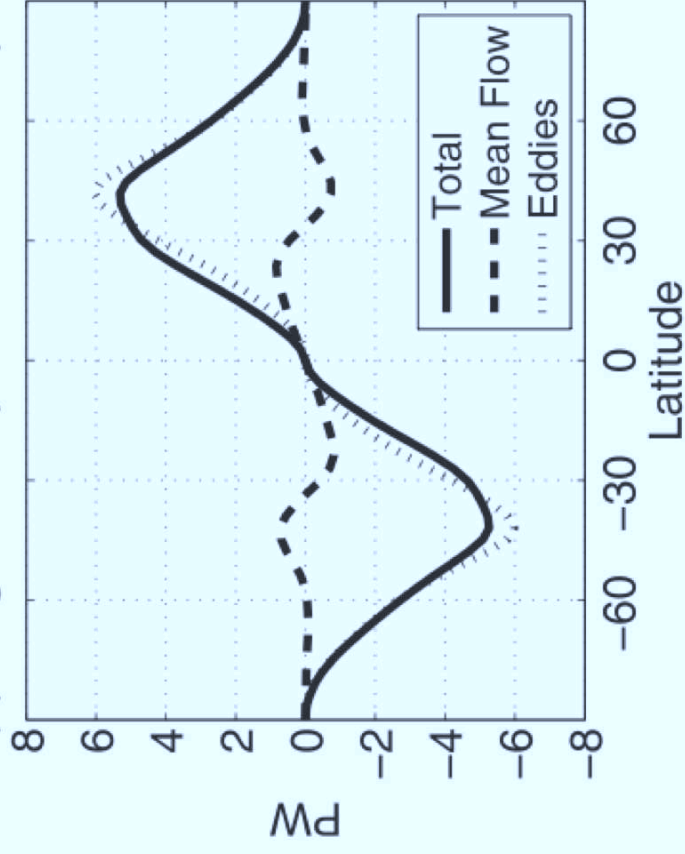
(b) Ridge Ocean Heat Transport



(a) Ridge Atmospheric Heat Transport



(b) Ridge Atmospheric Heat Transport



The rest of the paper is about why the total heat transport is slightly larger when the poles are icy.

Never says why circulation details affect ice!!!

$$\frac{dH_T}{d\phi} = 2\pi R^2 \cos \phi [S(\phi)a(\phi) - I(\phi)]$$

total heat  
transport  
change with  
latitude

=

Absorbed  
solar

-

Outgoing  
longwave

Circulations are wildly different but analysis is only in terms of top of atmosphere energy balance!

## 2-Box model of one hemisphere

Fluxes are divided by total incoming solar

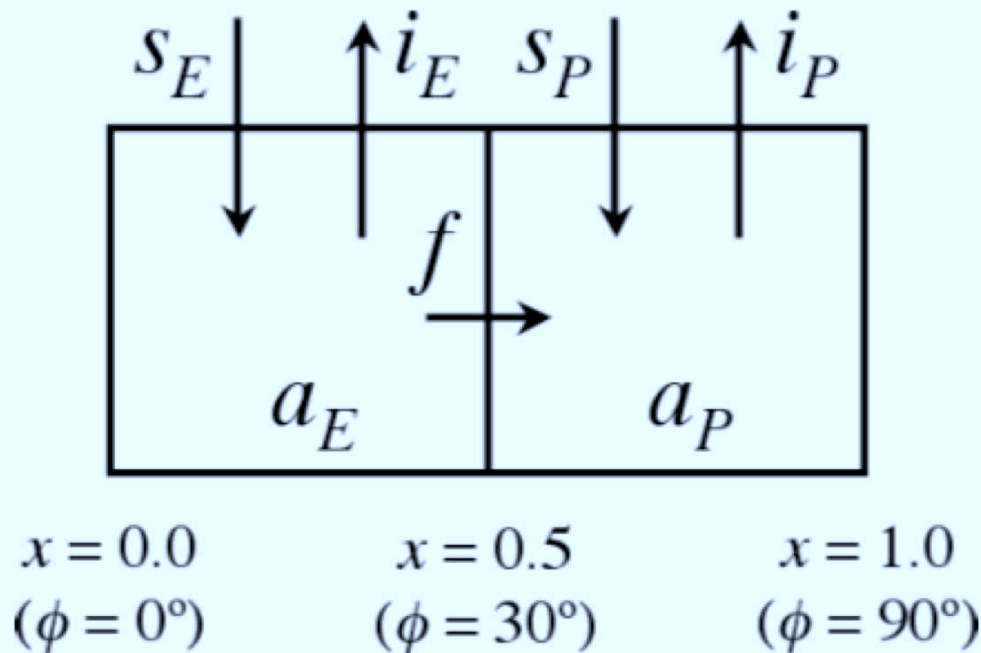
$s$  = absorbed solar

$i$  = outgoing longwave radiation

$f$  = transport at 30 deg

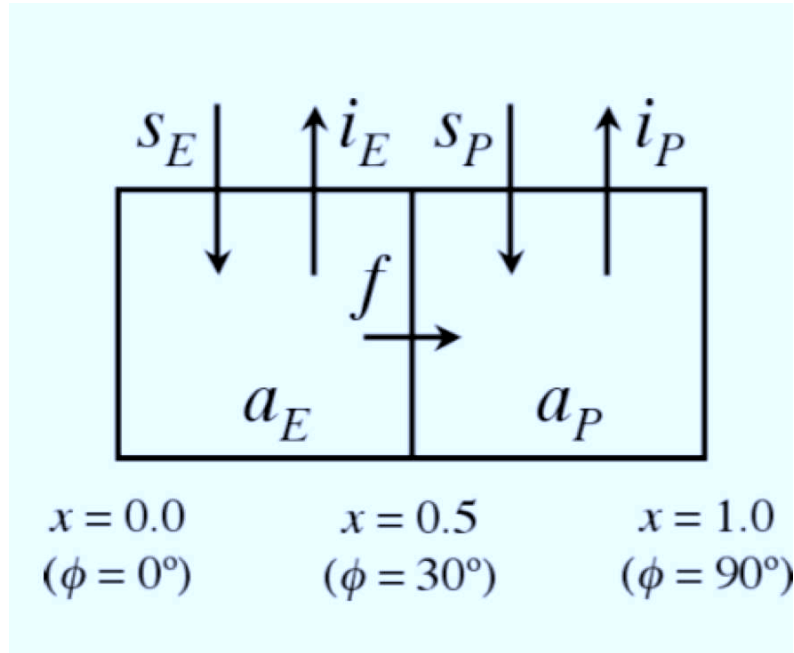
$a$  = co-albedo = 1-albedo

$x = \sin \phi$



Hemispheric energy balance requires the mean absorbed solar must equal mean OLR

$$\overline{s a} = \overline{i} \quad (\text{bar means box avg})$$



$$\Delta s = \overline{s_P} - \overline{s_E}$$

$$\Delta a = \overline{a_P} - \overline{a_E}$$

$$\Delta i = \overline{i_P} - \overline{i_E}.$$

Hemispheric energy balance also requires

$$f = - \left( \Delta s \overline{a} + \overline{s} \Delta a + \frac{1}{2} \Delta s \Delta a - \Delta i \right) \frac{\Delta x}{2}$$

After some algebra recognizing strong cancelation between solar absorption and outgoing longwave ...

	$-\Delta s \bar{a}$	$-\bar{s} \Delta a$	$-\frac{1}{2} \Delta s \Delta a$	$+\Delta i$	<i>Sum</i>	Two-box model $H_T$ at 30° (PW)	Coupled model $H_T$ at 30° (PW)
<i>Aqua</i> NH	0.240	0.086	-0.016	-0.021	0.289	6.30	6.25
<i>Ridge</i> NH	0.249	0.023	-0.004	0.002	0.270	5.88	5.81
<i>Drake</i> NH	0.250	0.024	-0.004	0.007	0.277	6.03	5.86
<i>Drake</i> SH	0.239	0.087	-0.016	-0.026	0.285	6.21	6.11

Biggest term is from differential heating by sun

But  $\Delta s$  and  $s$  are same for all cases - hence  $H_T$  differences are due primarily to co-albedo mean and pole-to-equator difference