

## Chapter 12: Structures & Properties of Ceramics

### ISSUES TO ADDRESS...

- How do the crystal structures of \_\_\_\_\_ materials differ from those for \_\_\_\_\_?
- How do \_\_\_\_\_ defects in ceramics differ from those defects found in metals?
- How are \_\_\_\_\_ accommodated in the ceramic lattice?
- In what ways are \_\_\_\_\_ phase diagrams different from phase diagrams for metals?
- How are the mechanical properties of ceramics \_\_\_\_\_, and how do they differ from those for metals?

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## Atomic Bonding in Ceramics

- Bonding:
  - \_\_\_\_\_
  - % ionic character \_\_\_\_\_ with difference in electronegativity of atoms.
- Degree of ionic character may be large or small:

IA												IIA												IIIA		IVA	VA	VIA	VIIA	0																		
H	Li	Na	K	Rb	Cs	Fr	Be	Mg	Ca	Sr	Ba	Ra	B	Al	Ga	In	Tl	Pb	Bi	Po	At	Rn	C	Si	Ge	Sn	Pb	N	P	As	Sb	Te	I	Xe	O	S	Se	Br	Kr	F	Cl	Ar	Ne					
2.1	1.0	0.9	0.8	0.8	0.7	0.7	1.5	1.2	1.0	1.0	1.0	0.9	2.0	1.5	1.6	1.7	1.8	1.9	2.0	2.1	2.2	2.2	2.2	2.5	1.8	1.8	1.8	1.8	3.0	2.1	2.1	2.1	2.1	2.5	3.0	3.5	2.0	2.0	2.4	2.8	4.0	3.0	3.0	3.0	3.0	3.0	3.0	-

CaF<sub>2</sub>: large (points to Ca)
 SiC: small (points to Si and C)

Adapted from Fig. 2.7, Callister & Rethwisch 8e. (Fig. 2.7 is adapted from Linus Pauling, *The Nature of the Chemical Bond*, 3rd edition, Copyright 1939 and 1940, 3rd edition. Copyright 1960 by Cornell University.) Chapter 12 - 2

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## Ceramic Crystal Structures

### Oxide structures

- oxygen anions \_\_\_\_\_ than metal cations
- close \_\_\_\_\_ oxygen in a \_\_\_\_\_ (usually \_\_\_\_\_)
- cations fit into \_\_\_\_\_ sites among \_\_\_\_\_ ions

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### Factors that Determine Crystal Structure

1. Relative sizes of ions – \_\_\_\_\_ :  
 --maximize the # of \_\_\_\_\_

Adapted from Fig. 12.1, Callister & Rethwisch 8e.

2. Maintenance of Charge Neutrality :  
 -- should be zero.  
 --Reflected in chemical formula:

$A_m X_p$   
 m, p values to achieve charge neutrality

$CaF_2$ :  $Ca^{2+}$  cation +  $F^-$  anions

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### Coordination # and Ionic Radii

- \_\_\_\_\_ # increases with  $\frac{r_{cation}}{r_{anion}}$

To form a \_\_\_\_\_ structure, how many anions can surround around a cation?

$\frac{r_{cation}}{r_{anion}}$	Coord #	Structure
< 0.155	2	linear
0.155 - 0.225	3	
0.225 - 0.414	4	tetrahedral
0.414 - 0.732	6	octahedral
0.732 - 1.0	8	

ZnS (zinc blende) Adapted from Fig. 12.4, Callister & Rethwisch 8e.

NaCl (sodium chloride) Adapted from Fig. 12.2, Callister & Rethwisch 8e.

CsCl (cesium chloride) Adapted from Fig. 12.3, Callister & Rethwisch 8e.

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### Computation of Minimum Cation-Anion Radius Ratio

- Determine \_\_\_\_\_  $r_{cation}/r_{anion}$  for an octahedral site (C.N. = \_\_\_\_\_)

$2r_{anion} + 2r_{cation} = \sqrt{2}a$

$2r_{anion} + 2r_{cation} = 2\sqrt{2}r_{anion}$

$r_{anion} + r_{cation} = \sqrt{2}r_{anion}$      $r_{cation} = (\sqrt{2} - 1)r_{anion}$

$\frac{r_{cation}}{r_{anion}} = \sqrt{2} - 1 = 0.414$

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### Bond Hybridization

Bond Hybridization is possible when there is significant \_\_\_\_\_ bonding

- \_\_\_\_\_
- For example for SiC
  - $X_{Si} = 1.8$  and  $X_C = 2.5$

% ionic character =  $100 \{1 - \exp[-0.25(X_{Si} - X_C)^2]\} = 11.5\%$

- ~ 89% \_\_\_\_\_ bonding
- Both Si and C prefer  $sp^3$  hybridization
- Therefore, for SiC, Si atoms occupy \_\_\_\_\_ sites

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### Example Problem: Predicting the Crystal Structure of FeO

- On the basis of ionic radii, what \_\_\_\_\_ would you predict for FeO?

Cation	Ionic radius (nm)
Al <sup>3+</sup>	0.053
Fe <sup>2+</sup>	0.077
Fe <sup>3+</sup>	0.069
Ca <sup>2+</sup>	0.100

Anion	Ionic radius (nm)
O <sup>2-</sup>	0.140
Cl <sup>-</sup>	0.181
F <sup>-</sup>	0.133

• Answer:  
 $\frac{r_{cation}}{r_{anion}} = \frac{0.077}{0.140} = 0.550$

based on this ratio,  
 -- coord # = \_\_\_\_\_ because  
 $0.414 < 0.550 < 0.732$   
 -- crystal structure is \_\_\_\_\_

Data from Table 12.3, Callister & Rethwisch 8e.

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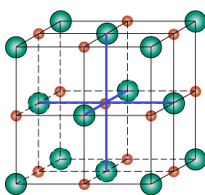
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### Rock Salt Structure

Same concepts can be applied to \_\_\_\_\_ solids in general.  
 Example: NaCl (rock salt) structure



- Na<sup>+</sup>  $r_{Na} = 0.102$  nm
  - Cl<sup>-</sup>  $r_{Cl} =$  \_\_\_\_\_ nm
- $r_{Na}/r_{Cl} =$  \_\_\_\_\_  
 $\therefore$  cations (Na<sup>+</sup>) prefer \_\_\_\_\_ sites

Adapted from Fig. 12.2, Callister & Rethwisch 8e.

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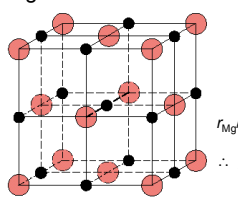
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### MgO and FeO

MgO and FeO also have the NaCl structure




● O<sup>2-</sup>  $r_{O} = 0.140 \text{ nm}$   
● Mg<sup>2+</sup>  $r_{Mg} = 0.072 \text{ nm}$

$r_{Mg}/r_{O} = \underline{\hspace{2cm}}$   
 $\therefore \underline{\hspace{2cm}}$  prefer octahedral sites

Adapted from Fig. 12.2, Callister & Rethwisch 8e.

So each Mg<sup>2+</sup> (or Fe<sup>2+</sup>)  $\underline{\hspace{2cm}}$  neighbor oxygen atoms

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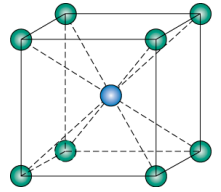
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### AX Crystal Structures

AX-Type Crystal Structures include NaCl, CsCl, and zinc blende

Cesium Chloride structure:




● Cs<sup>+</sup>  $r_{Cs^+} = 0.170$   
● Cl<sup>-</sup>  $r_{Cl^-} = 0.181$

$\therefore$  Since  $0.732 < \underline{\hspace{1cm}} < 1.0$ ,  
 $\underline{\hspace{1cm}}$  sites preferred

So each Cs<sup>+</sup> has  $\underline{\hspace{1cm}}$  neighbor Cl<sup>-</sup>

Adapted from Fig. 12.3, Callister & Rethwisch 8e.

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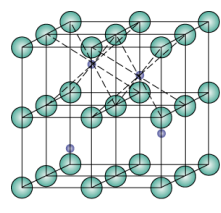
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### AX<sub>2</sub> Crystal Structures


Fluorite structure



- Calcium  $\underline{\hspace{1cm}}$  (CaF<sub>2</sub>)
- Cations in  $\underline{\hspace{1cm}}$  sites
- UO<sub>2</sub>, ThO<sub>2</sub>, ZrO<sub>2</sub>, CeO<sub>2</sub>
- $\underline{\hspace{1cm}}$  structure – positions of cations and anions reversed

● Ca<sup>2+</sup> ● F<sup>-</sup>

Adapted from Fig. 12.5, Callister & Rethwisch 8e.

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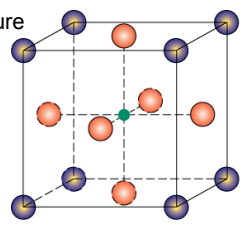
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### ABX<sub>3</sub> Crystal Structures

• \_\_\_\_\_ structure


Ex: complex oxide

\_\_\_\_\_



Adapted from Fig. 12.6, Callister & Rethwisch Be.

● Ti<sup>4+</sup> ● Ba<sup>2+</sup> ● O<sup>2-</sup>

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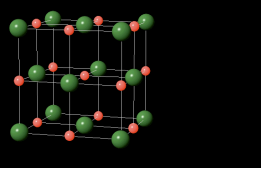
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### VMSE: Ceramic Crystal Structures

**Ceramic Crystal Structures**

This module allows you to observe and rotate (using mouse click-and-drag) unit cells for the seven common ceramic crystal structures listed in the left bar window. For each of these crystal structures, atomic/ionic packing arrangements for several crystallographic planes may be generated, which planes may also be rotated. Spinel and inverse spinel crystal structures may be displayed in terms of close-packed planes of oxygen ions and

Unit Cells	Sodium Chloride (NaCl)
NaCl	(110)
CaCl	(110)
ZnS	(111)
Diamond	(112)
Graphite	(123)
CaF <sub>2</sub>	(123)
BaTiO <sub>3</sub>	Reset
Substructure Spin	● Sodium
Close packed direction	● Chlorine
Material definition only	



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### Density Computations for Ceramics

Number of formula units/unit cell


$$\rho = \frac{n'(\sum A_C + \sum A_A)}{V_C N_A}$$

Volume of unit cell

\_\_\_\_\_ number

$\sum A_C$  = sum of atomic weights of \_\_\_\_\_

$\sum A_A$  = sum of atomic weights of \_\_\_\_\_

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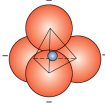
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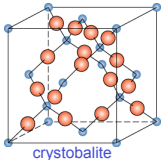
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### Silicate Ceramics

Most common \_\_\_\_\_




 Si<sup>4+</sup>  
 O<sup>2-</sup>



Adapted from Figs. 12.9-10, Callister & Rethwisch 8e  
cristobalite

- SiO<sub>2</sub> (silica) \_\_\_\_\_ forms are quartz, cristobalite, & tridymite
- The strong Si-O bonds lead to a high \_\_\_\_\_ temperature (1710°C) for this material

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### Silicates

Bonding of adjacent SiO<sub>4</sub><sup>4-</sup> accomplished by the sharing of common \_\_\_\_\_






Adapted from Fig. 12.12, Callister & Rethwisch 8e.

Mg<sub>2</sub>SiO<sub>4</sub>    Ca<sub>2</sub>MgSi<sub>2</sub>O<sub>7</sub>    Si<sub>3</sub>O<sub>9</sub><sup>6-</sup>

Presence of cations such as Ca<sup>2+</sup>, Mg<sup>2+</sup>, & Al<sup>3+</sup>

1. maintain charge \_\_\_\_\_, and
2. \_\_\_\_\_ bond SiO<sub>4</sub><sup>4-</sup> to one another

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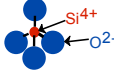
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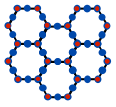
### Glass Structure

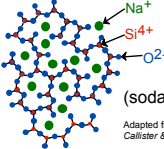
- Basic Unit: SiO<sub>4</sub><sup>4-</sup> tetrahedron
 



Glass is \_\_\_\_\_ (\_\_\_\_\_)


  - \_\_\_\_\_ is SiO<sub>2</sub> to which no impurities have been added
  - Other common \_\_\_\_\_ contain impurity ions such as Na<sup>+</sup>, Ca<sup>2+</sup>, Al<sup>3+</sup>, and B<sup>3+</sup>
- Quartz is \_\_\_\_\_  
SiO<sub>2</sub>:
 





(soda glass)

Adapted from Fig. 12.11, Callister & Rethwisch 8e

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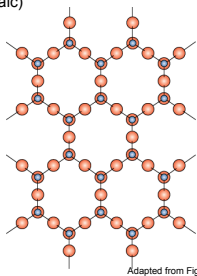
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### Layered Silicates

- Layered \_\_\_\_\_ (e.g., clays, mica, talc)
  - $\text{SiO}_4$  \_\_\_\_\_ connected together to form 2-D plane
- A net negative charge is associated with each  $(\text{Si}_2\text{O}_5)^{2-}$  unit
- Negative charge balanced by \_\_\_\_\_ plane rich in positively charged \_\_\_\_\_



Adapted from Fig. 12.13, Callister & Rethwisch 8e.  
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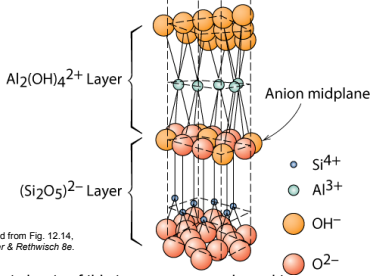
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### Layered Silicates (cont.)

- Kaolinite clay \_\_\_\_\_  $(\text{Si}_2\text{O}_5)^{2-}$  layer with  $\text{Al}_2(\text{OH})_4^{2+}$  layer



Adapted from Fig. 12.14, Callister & Rethwisch 8e.  
Note: Adjacent sheets of this type \_\_\_\_\_ bound to one another by \_\_\_\_\_.

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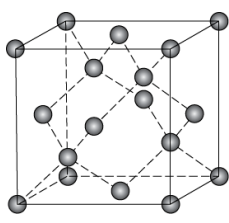
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### Polymorphic Forms of Carbon

#### Diamond

- tetrahedral bonding of carbon
  - \_\_\_\_\_
  - \_\_\_\_\_
- conductivity \_\_\_\_\_
- large single crystals – gem stones
- small \_\_\_\_\_ – used to grind/cut other materials
- \_\_\_\_\_ thin films
  - hard surface coatings – used for cutting tools, medical devices, etc.



Adapted from Fig. 12.15, Callister & Rethwisch 8e.  
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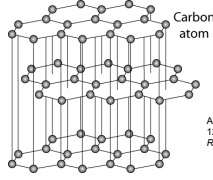
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### Polymorphic Forms of Carbon (cont)

\_\_\_\_\_ structure – parallel \_\_\_\_\_ arrays of carbon atoms



Carbon atom

Adapted from Fig. 12.17, Callister & Rethwisch 8e.

- weak van der Waal's forces between layers
- planes slide easily over one another -- good lubricant

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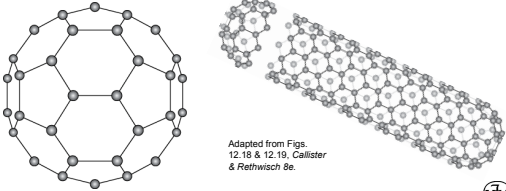
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### Polymorphic Forms of Carbon (cont)

#### Fullerenes and Nanotubes

- \_\_\_\_\_ – spherical cluster of 60 carbon atoms, C<sub>60</sub>
  - Like a soccer ball
- Carbon \_\_\_\_\_ – sheet of graphite rolled into a tube
  - Ends capped with fullerene \_\_\_\_\_



Adapted from Figs. 12.19 & 12.16, Callister & Rethwisch 8e.

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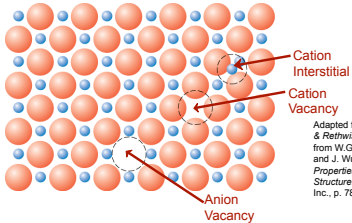
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### Point Defects in Ceramics (i)

- **Vacancies**
  - vacancies exist in \_\_\_\_\_ for both \_\_\_\_\_
- **Interstitials**
  - interstitials exist for \_\_\_\_\_
  - interstitials are not normally observed for \_\_\_\_\_ are large relative to the interstitial sites



Cation Interstitial

Cation Vacancy

Anion Vacancy

Adapted from Fig. 12.20, Callister & Rethwisch 8e. (Fig. 12.20 is from W.G. Moffatt, G.W. Peersall, and J. Wulff, *The Structure and Properties of Materials*, Vol. 1, Structure, John Wiley and Sons, Inc., p. 76.)

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### Point Defects in Ceramics (ii)

- Frenkel Defect
- Shottky Defect

Adapted from Fig.12.21, Callister & Rethwisch 8e. (Fig. 12.21 is from W.G. Moffatt, G.W. Pearsall, and J. Wulff: The Structure and Properties of Materials, Vol. 1, Structure, John Wiley and Sons, Inc., p. 78.)

- Equilibrium concentration of defects  $\propto e^{-Q_D/kT}$

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### Imperfections in Ceramics

- \_\_\_\_\_ (charge \_\_\_\_\_) must be maintained when impurities are present
- Ex: NaCl  $\text{Na}^+ \bullet \text{Cl}^-$
- Substitutional cation impurity
  - without impurity
  - $\text{Ca}^{2+}$  impurity
  - with impurity
- Substitutional anion impurity
  - without impurity
  - $\text{O}^{2-}$  impurity
  - with impurity

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### Ceramic Phase Diagrams

MgO-Al<sub>2</sub>O<sub>3</sub> diagram:

Adapted from Fig. 12.25, Callister & Rethwisch 8e.

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### Mechanical Properties

\_\_\_\_\_ materials are more brittle than \_\_\_\_\_.

Why is this so?

- Consider \_\_\_\_\_
  - In crystalline, by \_\_\_\_\_ motion
  - In highly ionic solids, dislocation motion is difficult
    - few \_\_\_\_\_
    - resistance to motion of ions of like charge (e.g., anions) past one another

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### Flexural Tests – Measurement of Elastic Modulus

- Room *T* behavior is usually \_\_\_\_\_, with \_\_\_\_\_ failure.
- \_\_\_\_\_ often used.
- tensile tests are difficult for \_\_\_\_\_ materials.

Adapted from Fig. 12.32, Callister & Rethwisch 8e.

- Determine \_\_\_\_\_ according to:

$$E = \frac{F}{\delta} \frac{L^3}{4bd^3} \quad (\text{rect. cross section})$$

$$E = \frac{F}{\delta} \frac{L^3}{12\pi R^4} \quad (\text{circ. cross section})$$

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### Flexural Tests – Measurement of Strength

- \_\_\_\_\_ test to measure room-*T* flexural strength.

- \_\_\_\_\_ strength:

$$\sigma_{fs} = \frac{3F_f L}{2bd^2} \quad (\text{rect. } \underline{\hspace{2cm}})$$

$$\sigma_{fs} = \frac{F_f L}{\pi R^3} \quad (\text{circ. } \underline{\hspace{2cm}})$$

• Typical values:

Material	$\sigma_{fs}$ (MPa)	$E$ (GPa)
Si nitride	250-1000	304
Si carbide	100-820	345
Al oxide	275-700	393
glass (soda-lime)	69	69

Data from Table 12.5, Callister & Rethwisch 8e.

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### SUMMARY

- Interatomic bonding in ceramics is ionic and/or covalent.
- Ceramic crystal structures are based on:
  - maintaining charge neutrality
  - cation-anion radii ratios.
- Imperfections
  - Atomic point: vacancy, interstitial (cation), Frenkel, Schottky
  - Impurities: substitutional, interstitial
  - Maintenance of charge neutrality
- Room-temperature mechanical behavior – flexural tests
  - linear-elastic; measurement of elastic modulus
  - brittle fracture; measurement of flexural modulus

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